



上海科技大学
ShanghaiTech University

CS283: Robotics Spring 2026: Vision II

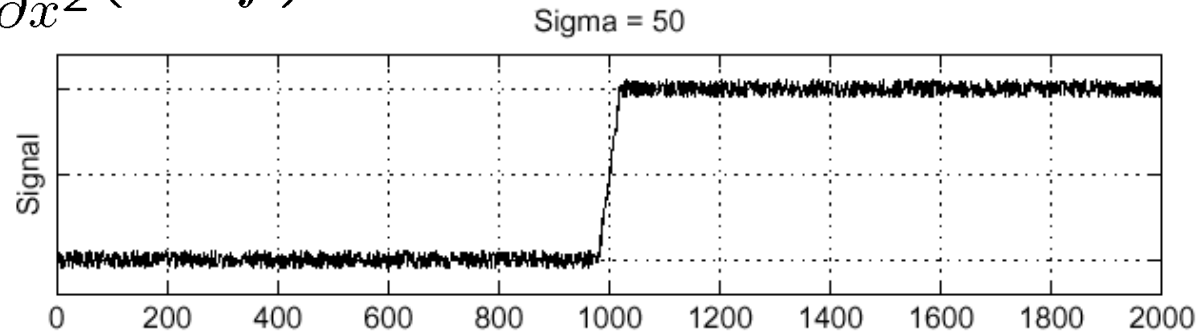
Sören Schwertfeger

ShanghaiTech University

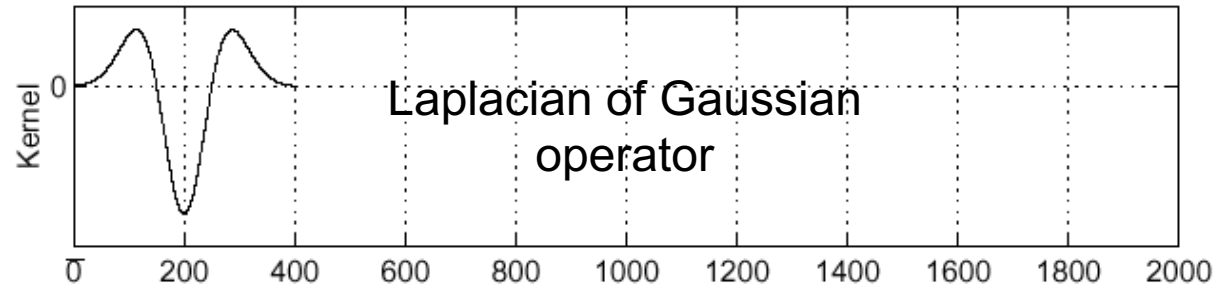
The Canny Edge Detector

- Consider $\frac{\partial^2}{\partial x^2}(h \star f)$

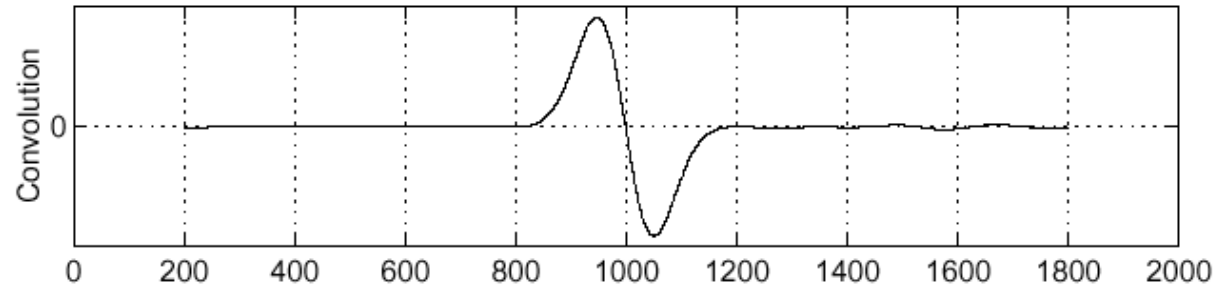
f



$\frac{\partial^2}{\partial x^2}h$

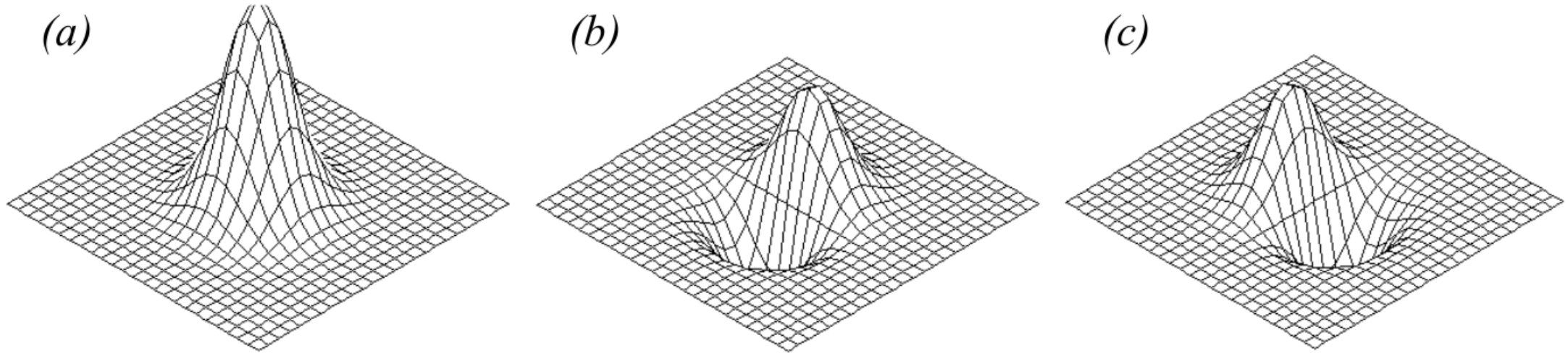


$(\frac{\partial^2}{\partial x^2}h) \star f$



- Where is the edge?
- Zero-crossings of bottom graph

2D Canny edge detector



$$G_{\sigma}(x, y) = G_{\sigma}(x)G_{\sigma}(y) \quad f_V(x, y) = G'_{\sigma}(x)G_{\sigma}(y) \quad f_H(x, y) = G'_{\sigma}(y)G_{\sigma}(x)$$

- Two perpendicular filters:

- Convolve image $I(x, y)$ with $f_V(x, y)$ and $f_H(x, y)$ – obtaining $R_V(x, y)$ and $R_H(x, y)$
- Use square of gradient magnitude: $R(x, y) = R_V^2(x, y) + R_H^2(x, y)$
- Mark peaks in $R(x, y)$ above a threshold

The Canny edge detector



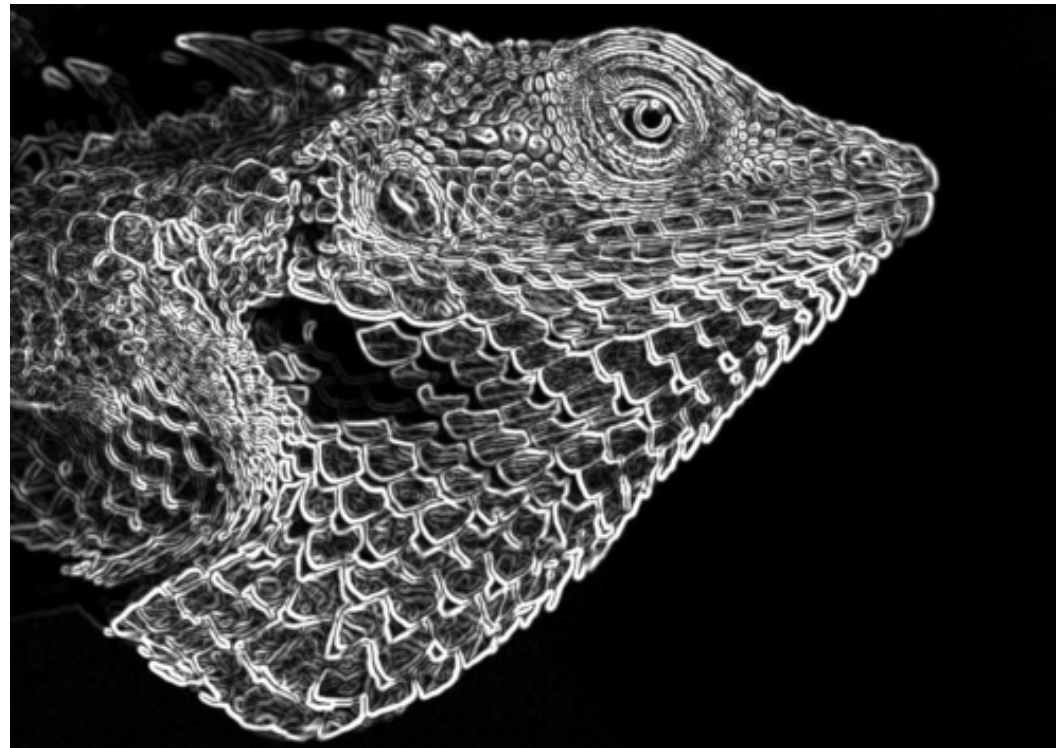
The Canny edge detector

- Image has been reduced to grayscale, and a 5x5 Gaussian filter with $\sigma=1.4$ has been applied.



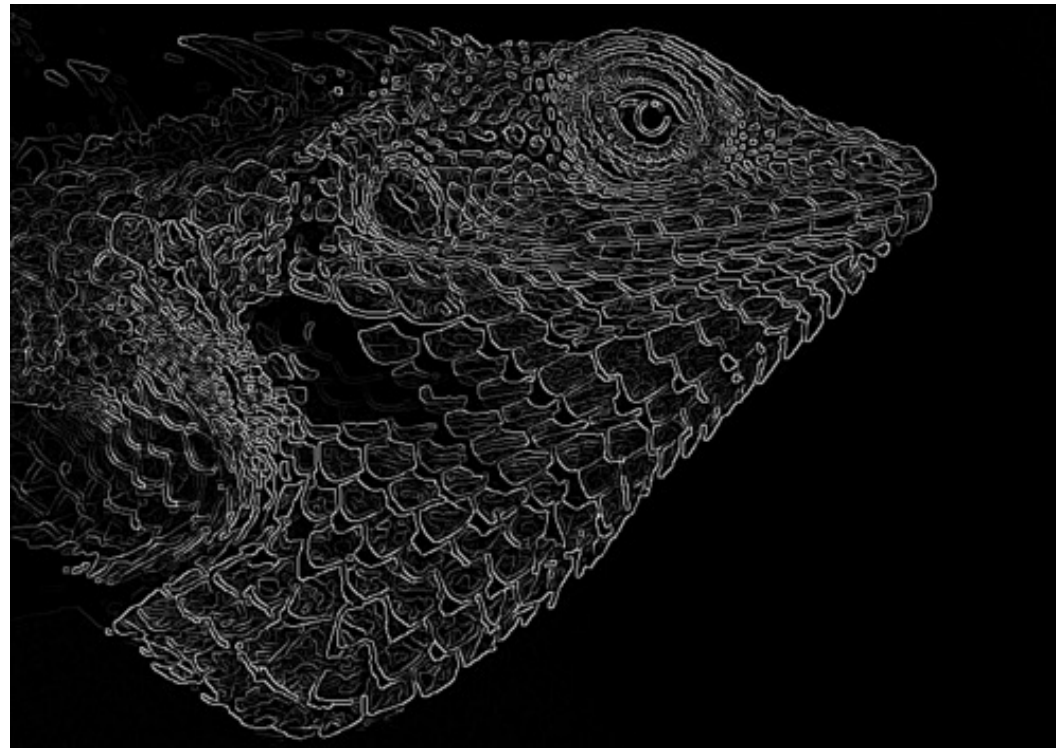
The Canny edge detector

The intensity gradient of the previous image. The edges of the image have been handled by replicating.



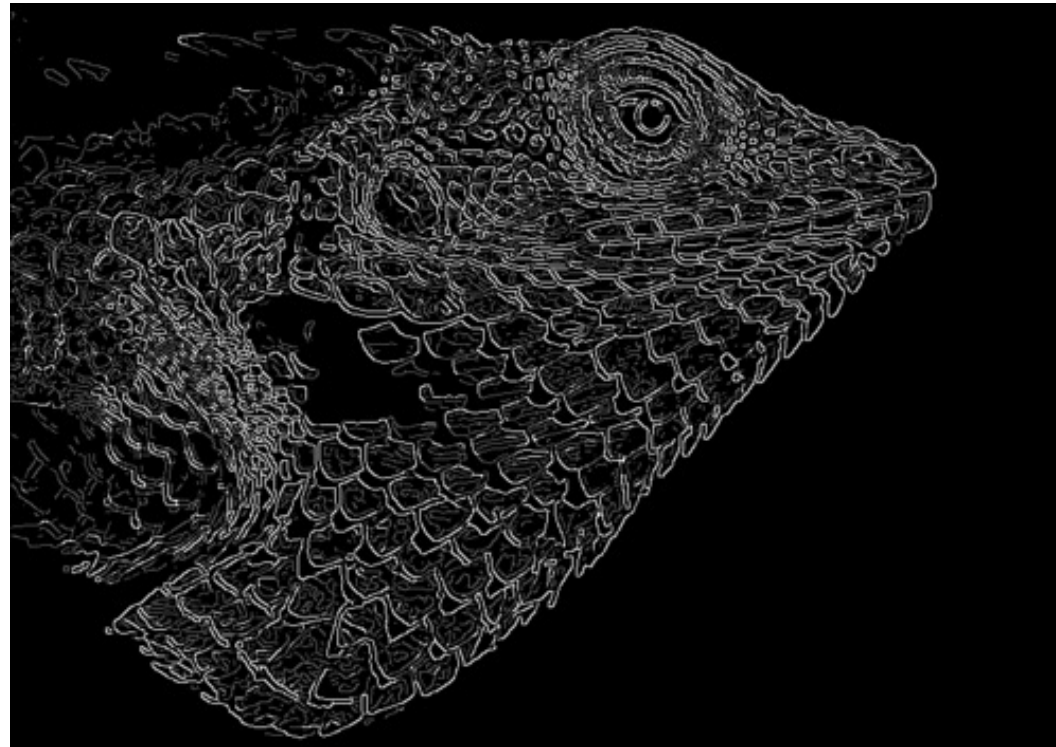
The Canny edge detector

Non-maximum suppression applied to the previous image



The Canny edge detector

Double thresholding applied to the previous image. Weak pixels are those with a gradient value between 0.1 and 0.3. Strong pixels have a gradient value greater than 0.3.



The Canny edge detector

Hysteresis: Finalize the detection of edges by suppressing all the other edges that are weak and not connected to strong edges (8-neighborhood).

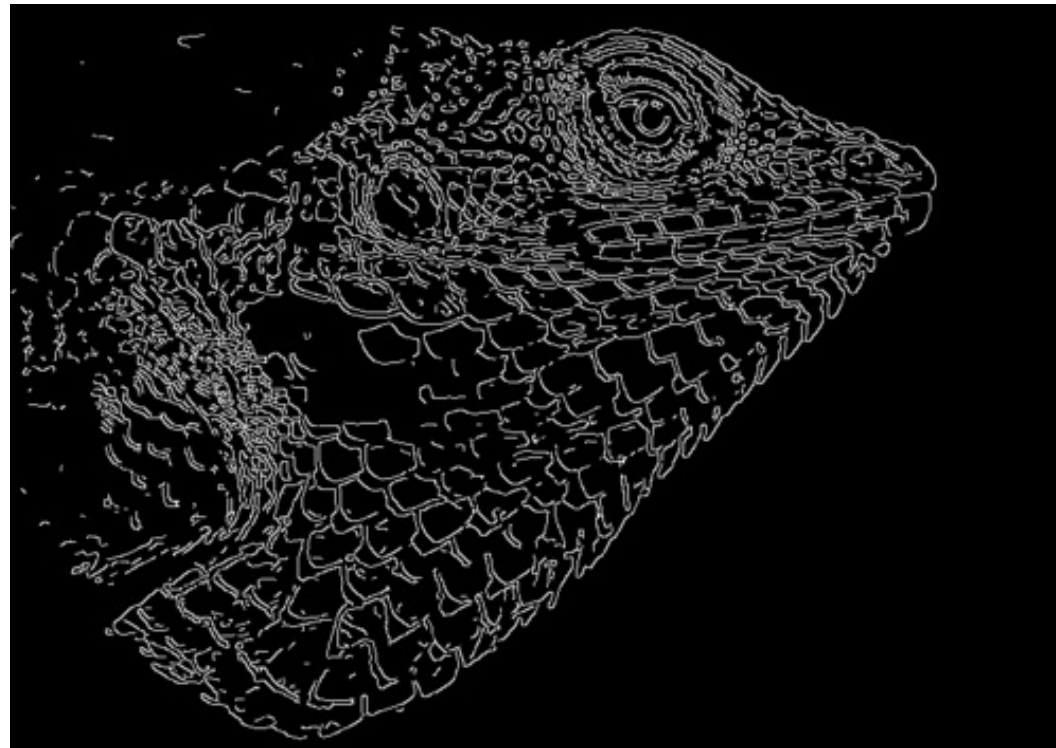


IMAGE FEATURES

- Lines
- Points
 - Harris
 - SIFT

Example: Build a Panorama



This panorama was generated using **AUTOSTITCH** (freeware), available at <http://www.cs.ubc.ca/~mbrown/autostitch/autostitch.html>

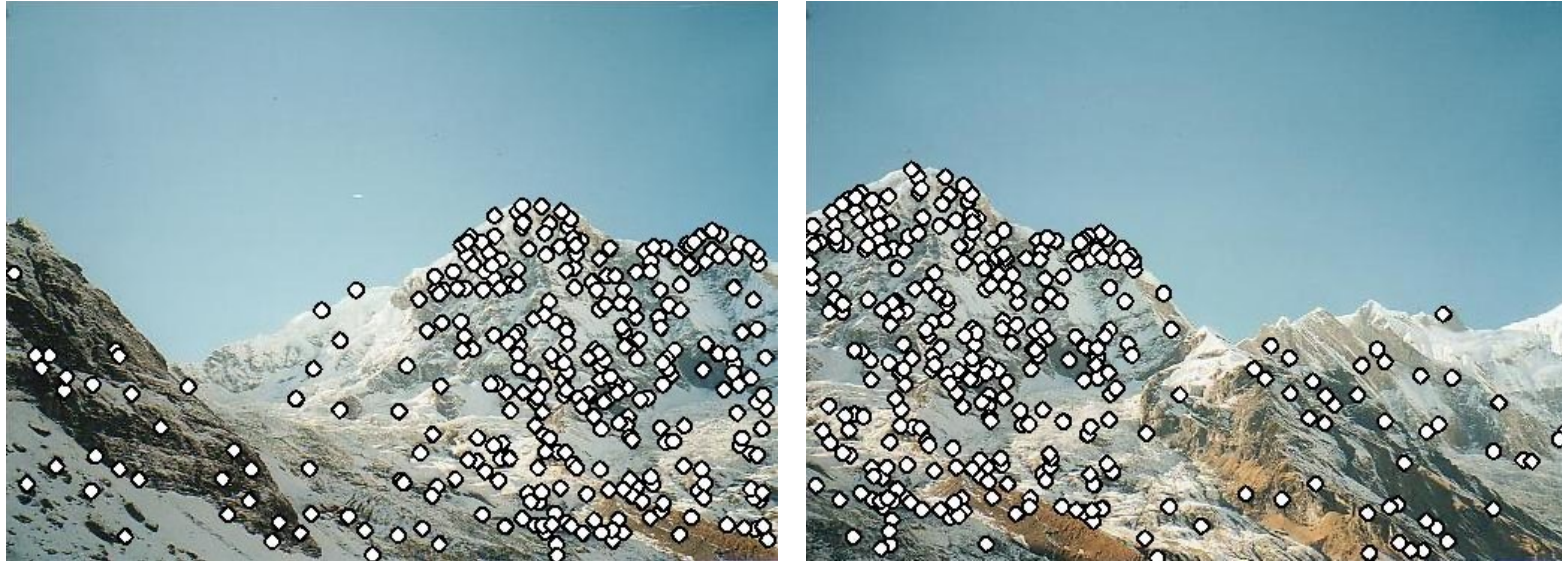
How do we build panorama?

- We need to match (align) images



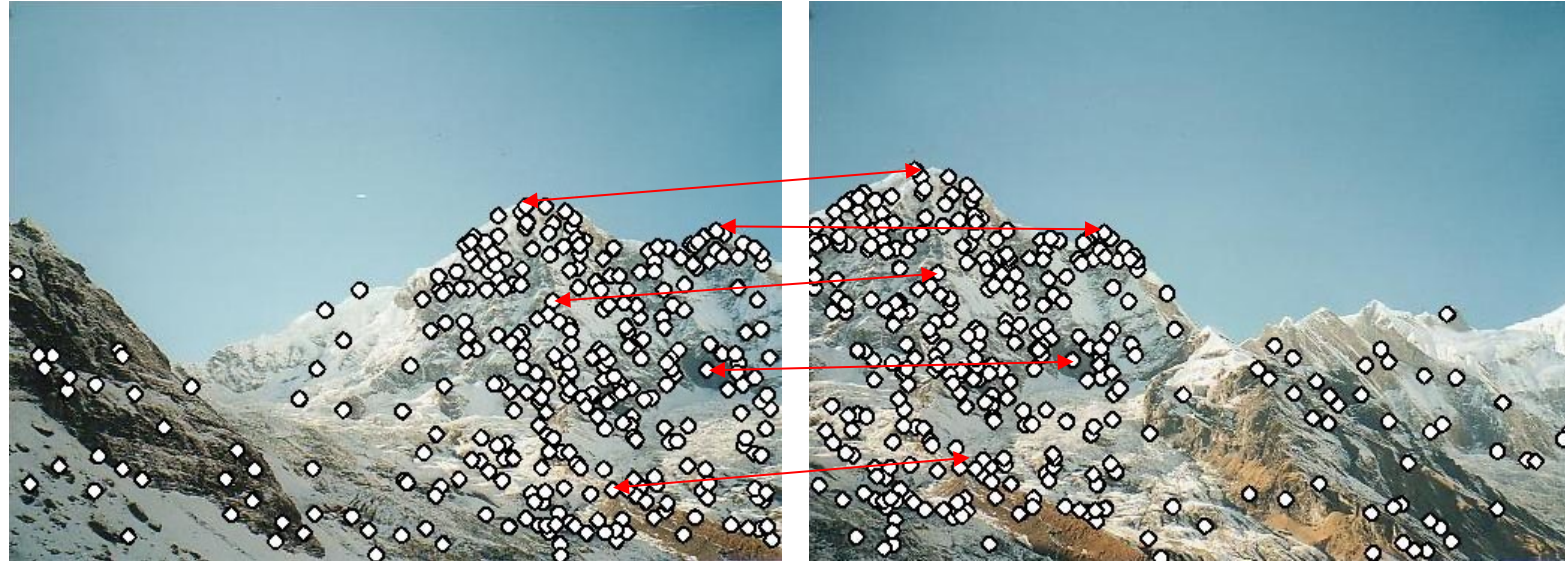
Matching with Features

- Detect feature points in both images



Matching with Features

- Detect feature points in both images
- Find corresponding pairs
 - Use RANSAC to find inliers and outliers



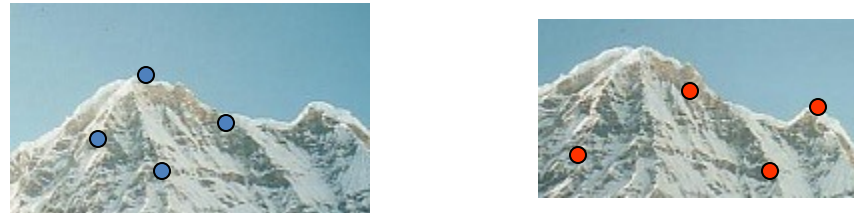
Matching with Features

- Detect feature points in both images
- Find corresponding pairs
- Use these pairs to align images



Matching with Features

- Problem 1:
 - Detect the *same* point *independently* in both images

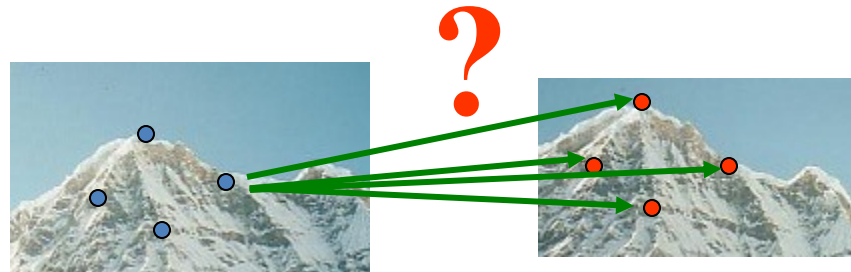


no chance to match!

We need a repeatable detector

Matching with Features

- Problem 2:
 - For each point correctly recognize the corresponding one



We need a reliable and distinctive descriptor

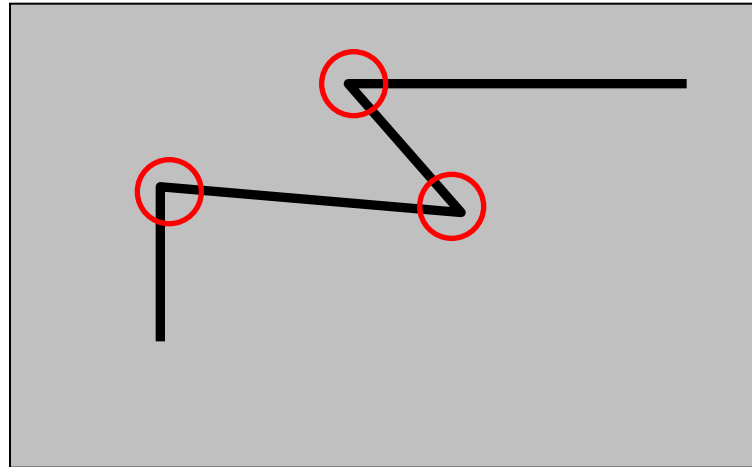
More motivation...

- Feature points are used also for:
 - Robot navigation
 - Object recognition
 - Image alignment (panoramas)
 - 3D reconstruction
 - Motion tracking
 - Indexing and database retrieval -> Google Images
 - ... other

Most Famous Feature Detectors

- Overview
 - Harris Detector (1988)
 - SIFT Detector (2004)

HARRIS CORNER DETECTOR



C.Harris, M.Stephens. "A Combined Corner and Edge Detector". 1988

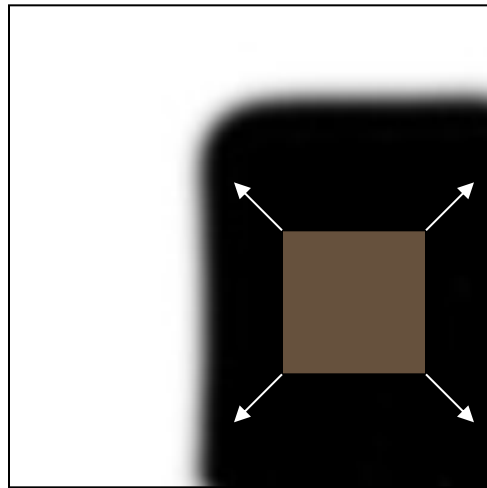
Finding Corners



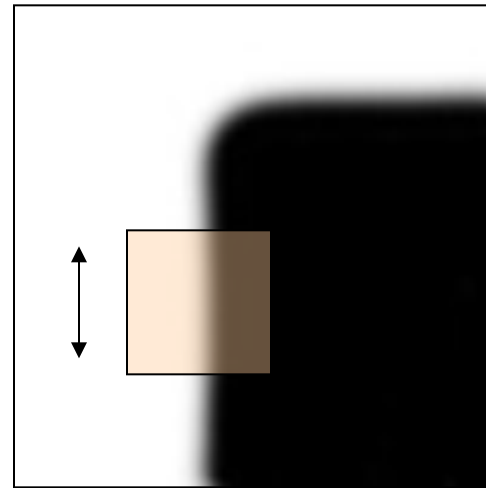
- Key property: in the region around a corner, image gradient has two or more dominant directions
- Corners are repeatable and distinctive

The basic idea

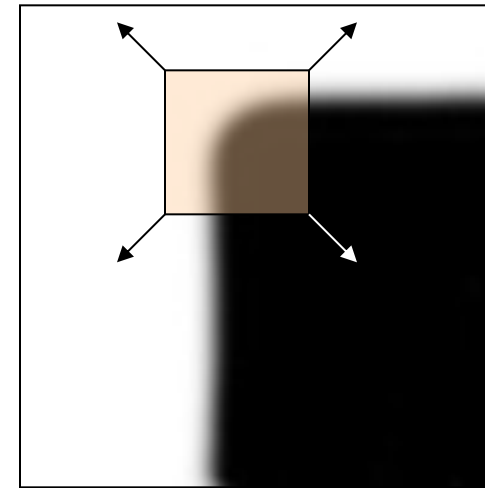
- We should easily recognize the point by looking through a small window
- Shifting a window in *any direction* should give a *large change* in intensity
- => define a corner response function



“flat” region:
no change in all
directions



“edge”:
no change along the
edge direction



“corner”:
significant change in
all directions

How do we implement this?

- Let I be a grayscale image. Consider taking an image patch centered on (u,v) and shifting it by (x,y) . The Sum of Squared Differences between these two patches is given by:

$$SSD(x, y) = \sum_u \sum_v ((I(u, v)) - I(u + x, v + y))^2$$

- $I(u + x, v + y)$ can be approximated by a first order Taylor expansion. Let I_x and I_y be the partial derivatives of I , such that

$$I(u + x, v + y) \approx I(u, v) + I_x(u, v)x + I_y(u, v)y$$

- This produces the approximation

$$SSD(x, y) \approx \sum_u \sum_v (I_x(u, v)x + I_y(u, v)y)^2$$

- Which can be written in a matrix form as $SSD(x, y) \approx \begin{bmatrix} x & y \end{bmatrix} M \begin{bmatrix} x \\ y \end{bmatrix}$

How do we implement this?

$$SSD(x, y) \approx \begin{bmatrix} x & y \end{bmatrix} M \begin{bmatrix} x \\ y \end{bmatrix}$$

- M is the “second moment matrix”
- Since M is symmetric, we can rewrite M as

$$M = \sum_u \sum_v \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix} = \begin{bmatrix} \sum \sum I_x^2 & \sum \sum I_x I_y \\ \sum \sum I_x I_y & \sum \sum I_y^2 \end{bmatrix}$$

where λ_1 and λ_2 are the eigenvalues of M

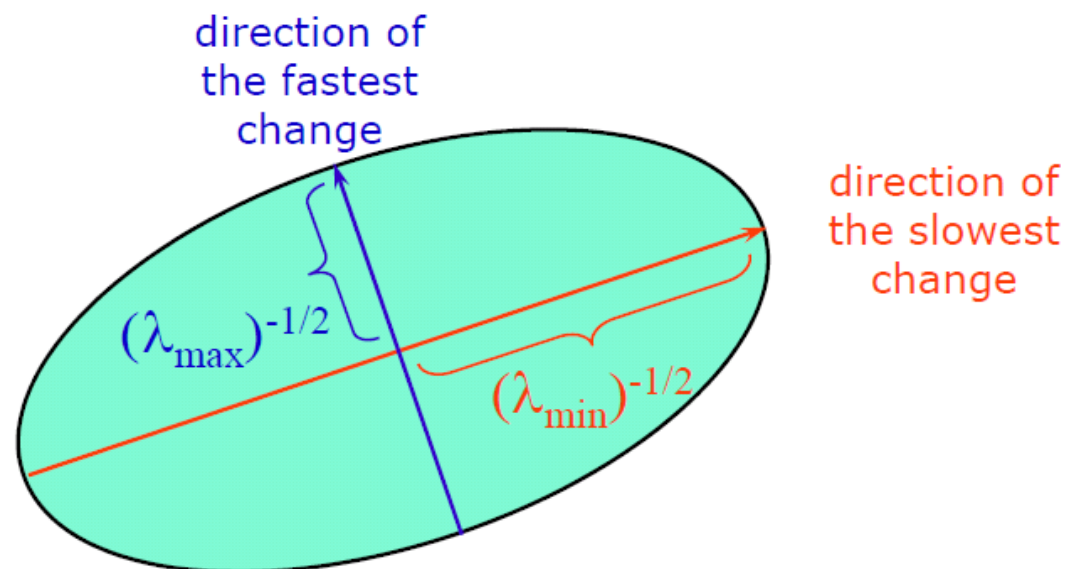
$$M = R^{-1} \begin{bmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{bmatrix} R$$

How do we implement this?

- As mentioned before, a corner is characterized by a large variation of in all directions of the vector (x,y) . The Harris detector analyses the eigenvalues of M to decide if we are in presence of a corner or not.
- We can visualize M as an ellipse with axis lengths determined by the eigenvalues and orientation determined by R

Ellipse equation:

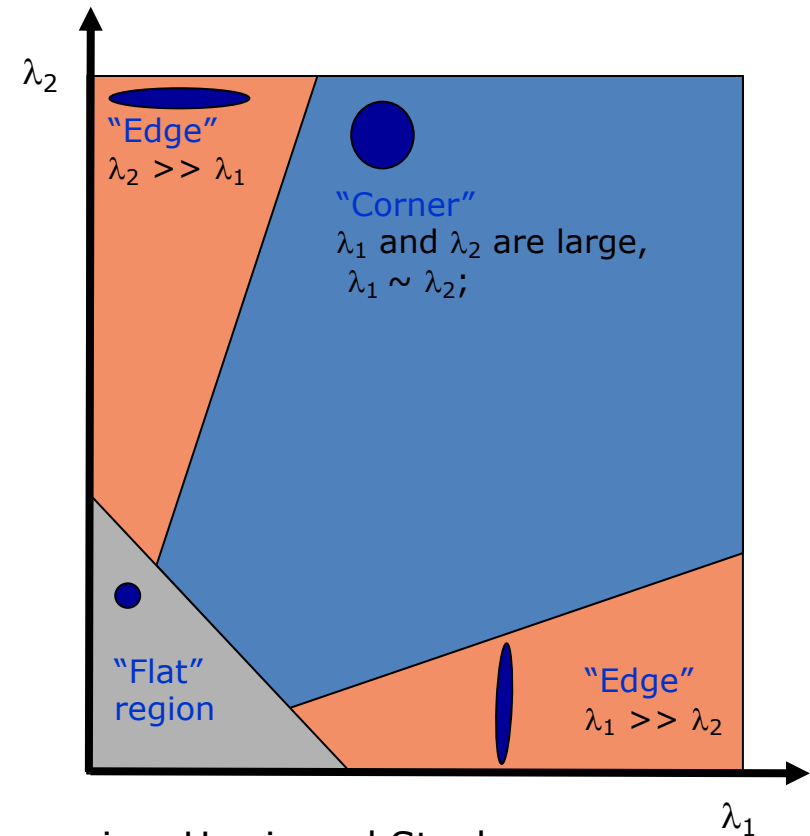
$$[u \ v] M \begin{bmatrix} u \\ v \end{bmatrix} = \text{const}$$



Corner response function

Based on the magnitudes of the eigenvalues, the following inferences can be made based on this argument:

- If both λ_1 and λ_2 are small, SSD is almost constant in all directions (i.e. we are in presence of a flat region).
- If either $\lambda_1 \gg \lambda_2$ or $\lambda_2 \gg \lambda_1$, we are in presence of an edge: SSD has a large variation only in one direction, which is the one perpendicular to the edge.
- If both λ_1 and λ_2 are large, SSD has large variations in all directions and then we are in presence of a corner.



Because the calculation of the eigenvalues is computationally expensive, Harris and Stephens suggested the use of the following **"cornerness function"** instead:

$$C = \lambda_1 \lambda_2 - \kappa (\lambda_1 + \lambda_2)^2 = \det(M) - \kappa \cdot \text{trace}^2(M)$$

Where κ is a between 0.04 and 0.15

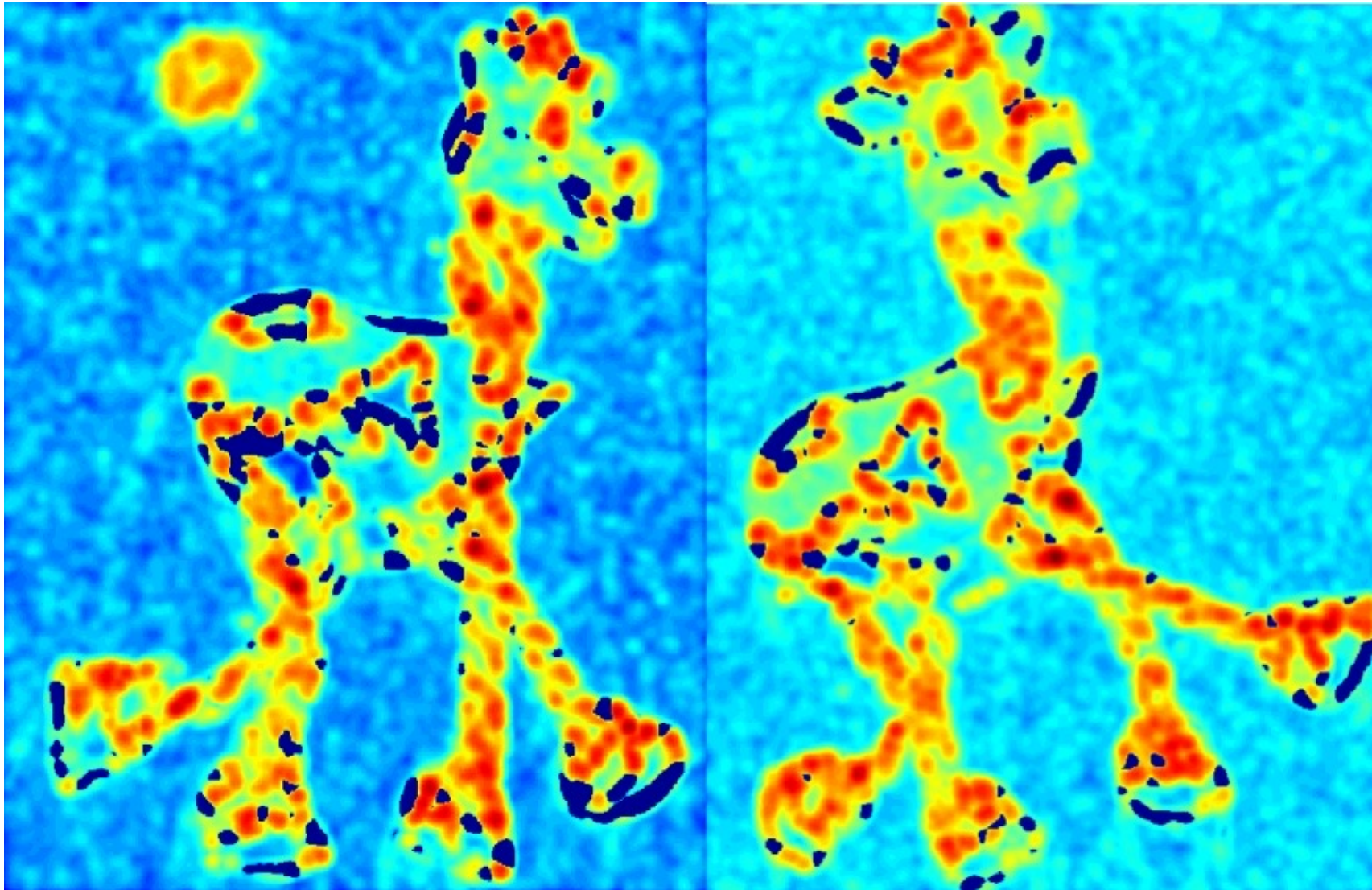
- Finally, the last step of the Harris corner detector consists in extracting the local maxima of the cornerness function

Harris Detector: Workflow



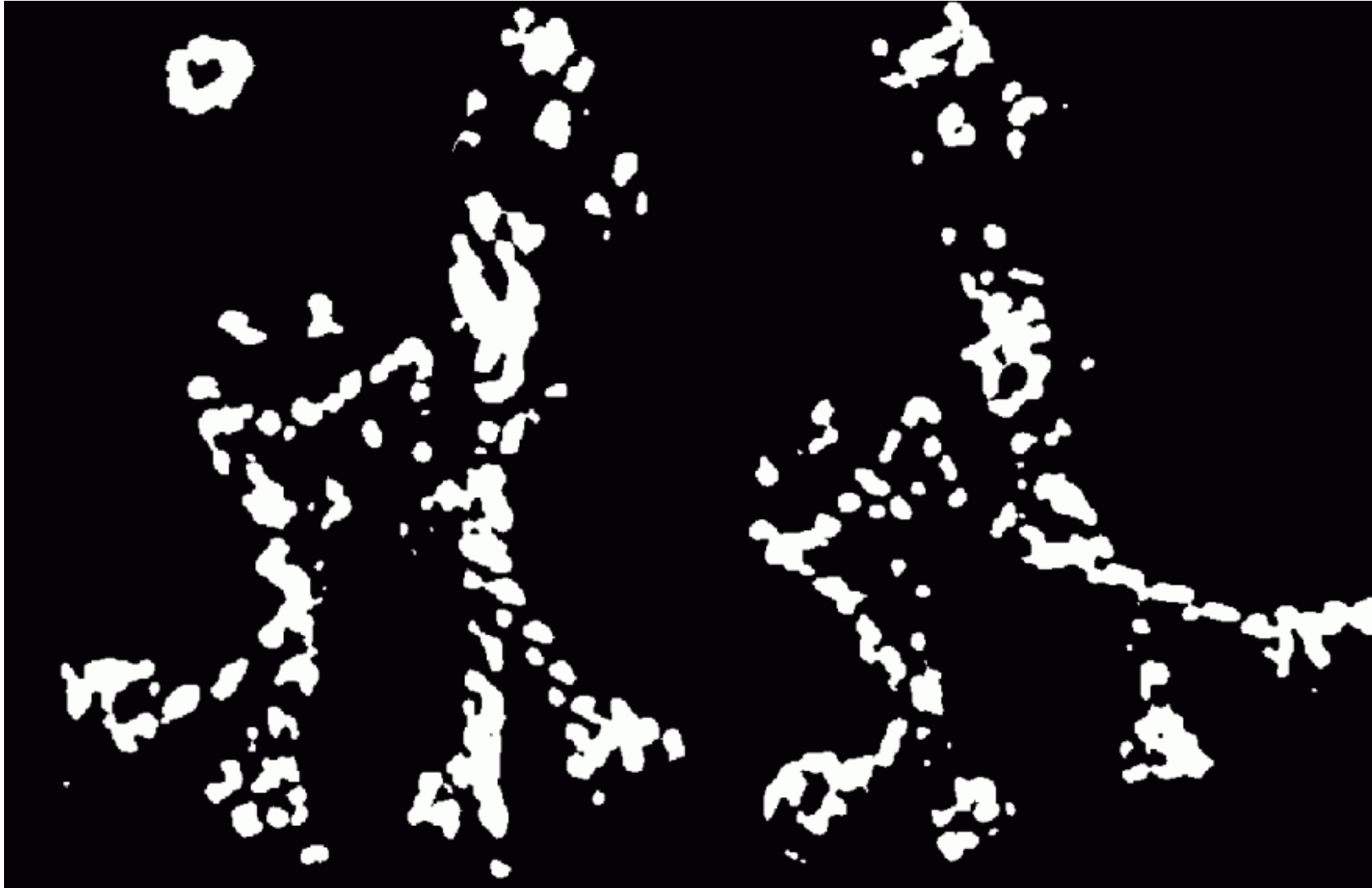
Harris Detector: Workflow

- Compute corner response R



Harris Detector: Workflow

- Find points with large corner response: $R >$ threshold



Harris Detector: Workflow

- Take only the points of local maxima of R



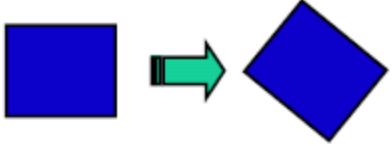
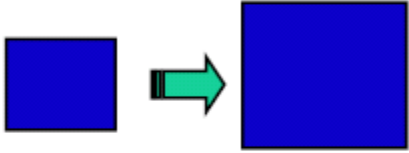

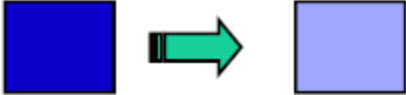
Harris Detector: Workflow



Harris detector: properties

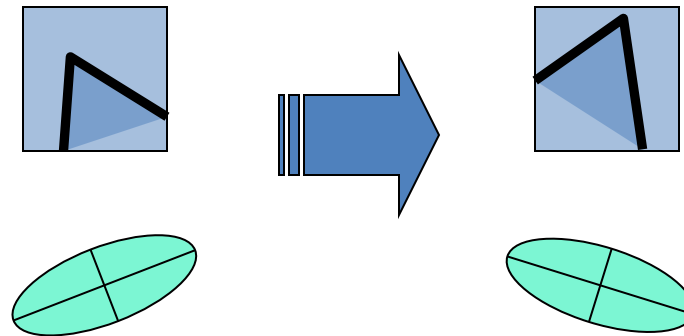
- How does the Harris detector behave to image transformations?
- Will we be able to re-detect the same corners under
 - Rotations
 - View-point changes
 - Zoom changes
 - Illumination changes?
- In order to answer these questions, we need a model of these transformations.
- The detector can then be modified to be invariant to such transformations

Models of Image Change

- **Geometric**
 - **Rotation**
 - **Scale**
 - **Affine**
valid for locally planar object
- **Photometric**
 - **Affine intensity change** ($I \rightarrow aI + b$)

Harris Detector: Some Properties

- Rotation invariance

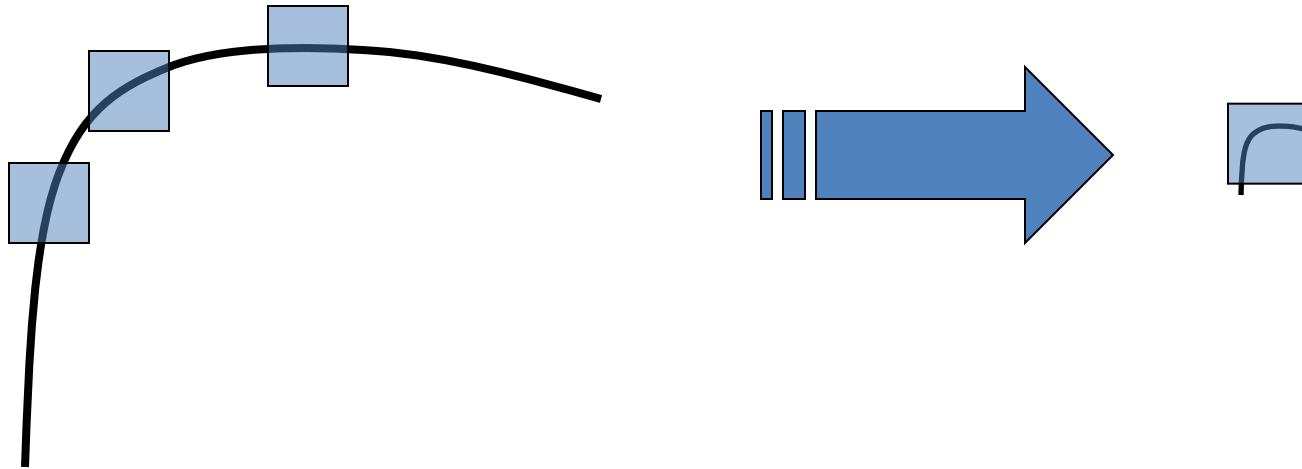


Ellipse rotates but its shape (i.e. eigenvalues) remains the same

Corner response R is invariant to image rotation

Harris Detector: Some Properties

- But: non-invariant to *image scale*!



All points will be
classified as **edges**

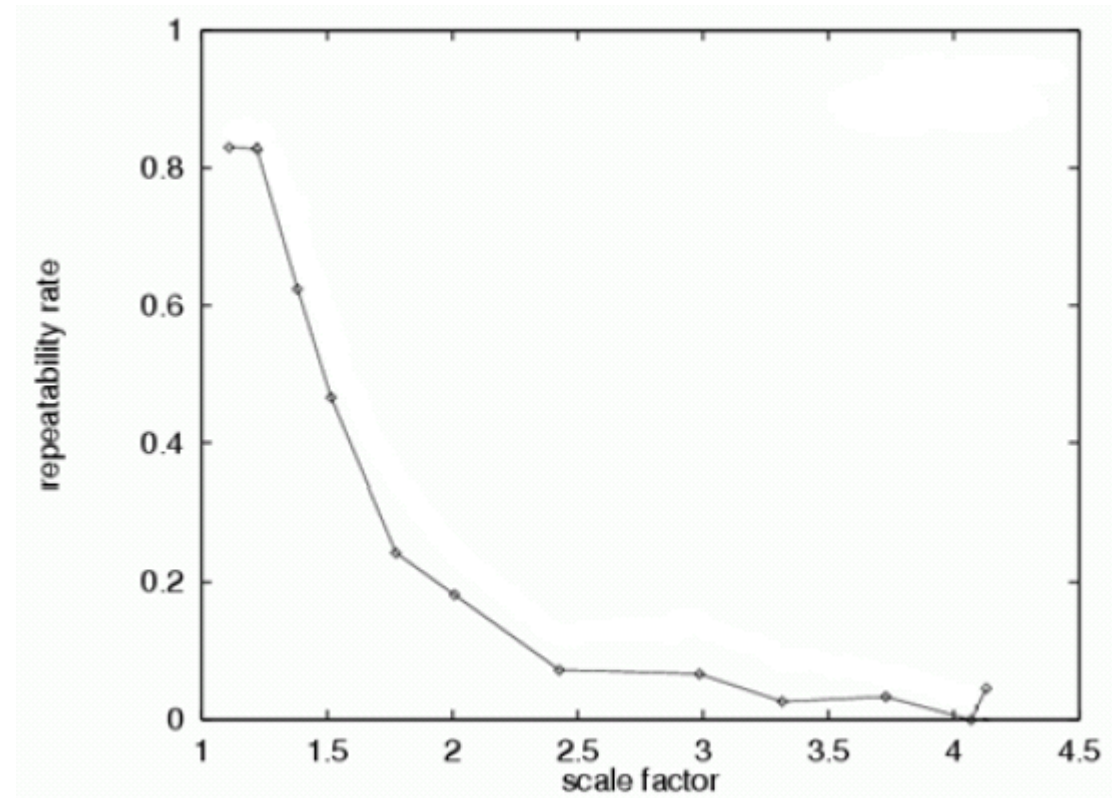
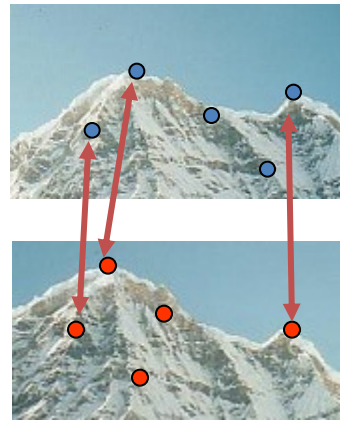
Corner !

Harris Detector: Some Properties

- Quality of Harris detector for different scale changes

Repeatability rate:

$$\frac{\# \text{ correspondences}}{\# \text{ possible correspondences}}$$

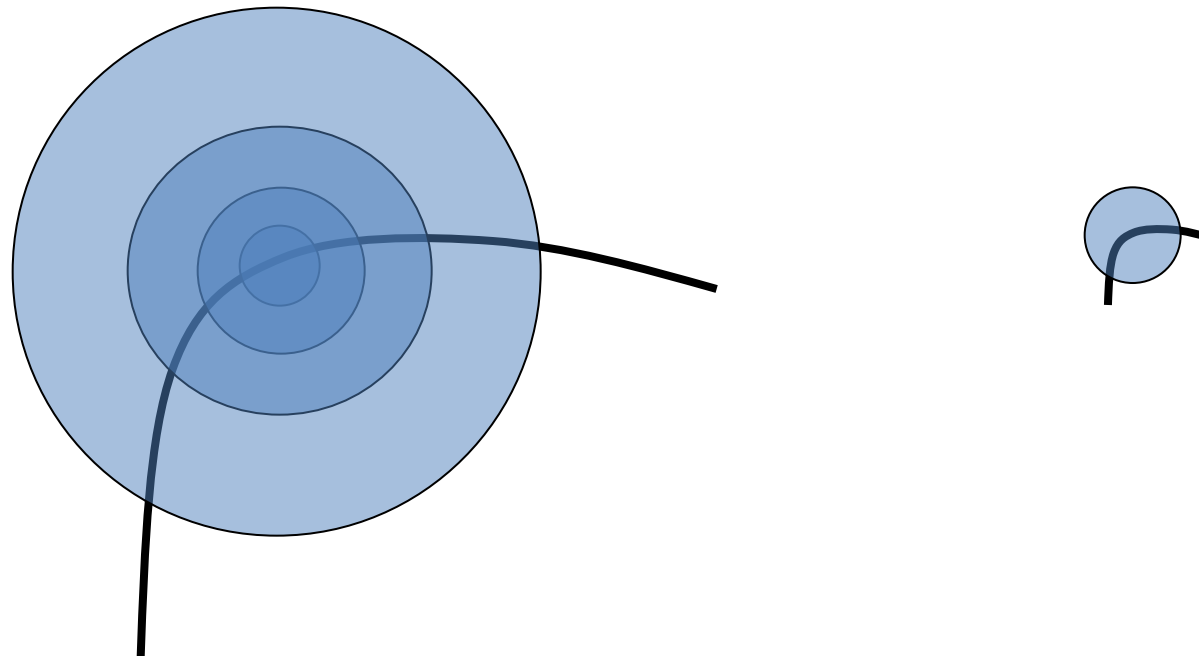


Summary on Harris properties

- Harris detector is an approach for detecting and extracting corners (i.e. points with high intensity changes in all directions)
- The detection is Invariant to
 - Rotation
 - Linear intensity changes
 - However, to make the matching invariant to these we need an appropriate matching criterion (for example, SSD is not Rotation nor affine invariant!)
- The detection is NOT invariant to
 - Scale changes
 - Geometric affine changes (Intuitively, an affine transformation distorts the neighborhood of the feature along the x and y directions and, accordingly, a corner can get reduced or increased its curvature)

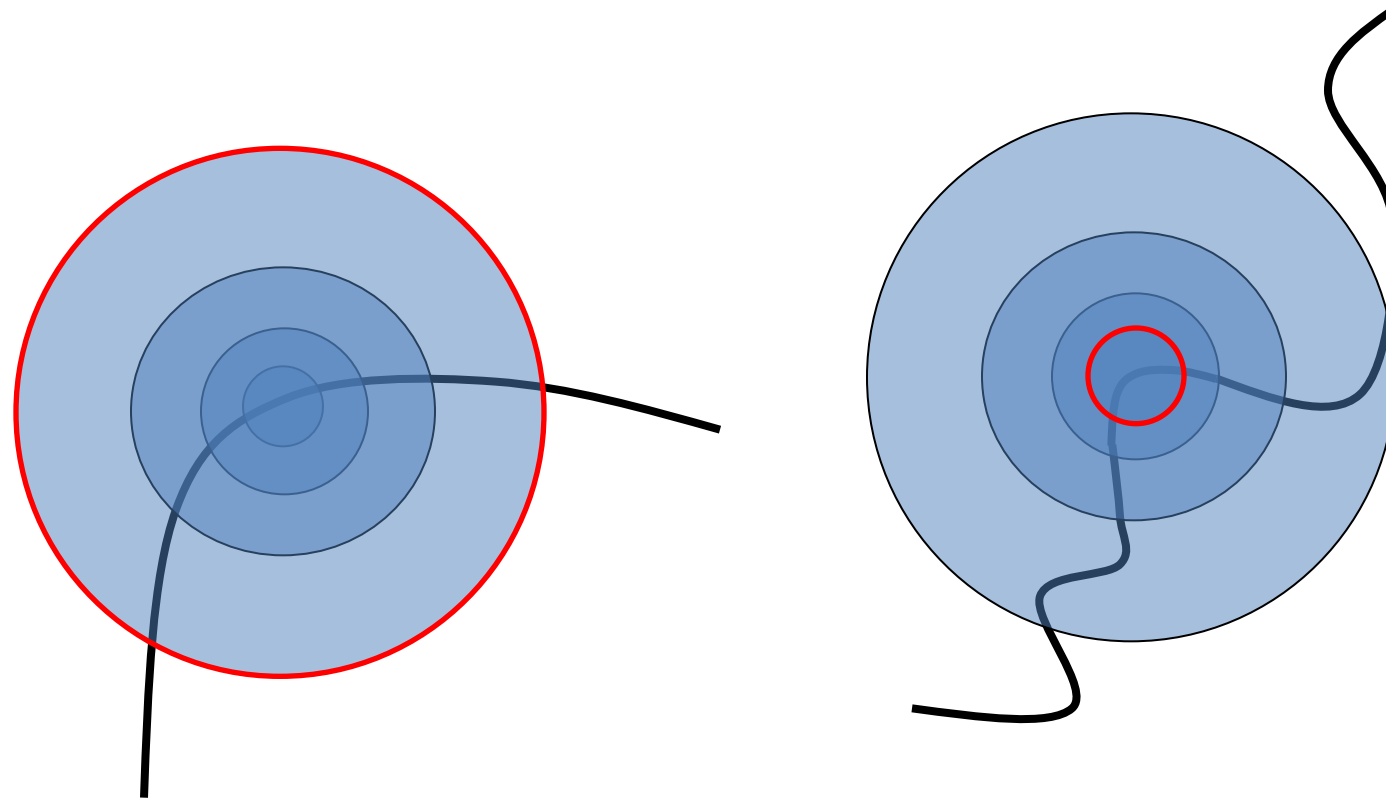
Scale Invariant Detection

- Consider regions (e.g. circles) of different sizes around a point
- Regions of corresponding sizes will look the same in both images



Scale Invariant Detection

- The problem: how do we choose corresponding circles *independently* in each image?

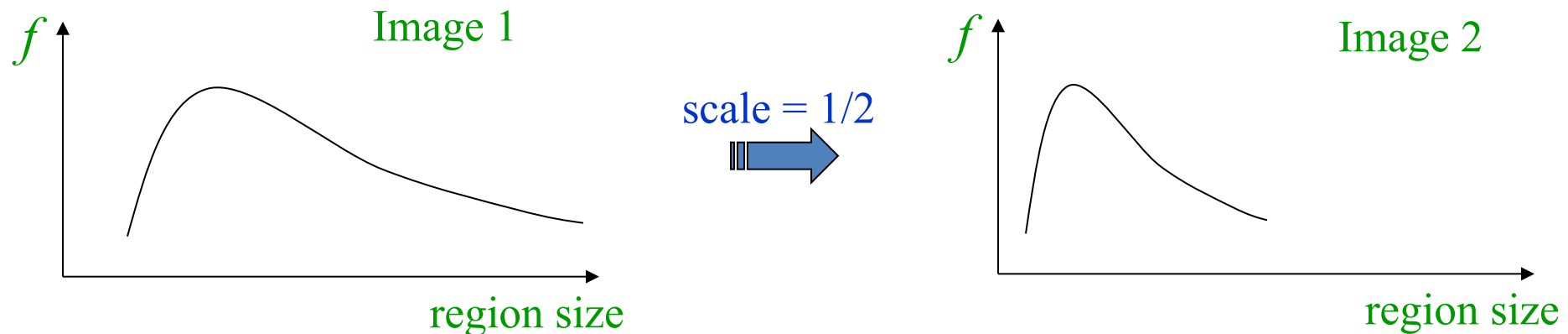


Scale Invariant Detection

- Solution:
 - Design a function on the region (circle), which is “scale invariant” (the same for corresponding regions, even if they are at different scales)

Example: average intensity. For corresponding regions (even of different sizes) it will be the same.

- For a point in one image, we can consider it as a function of region size (circle radius)



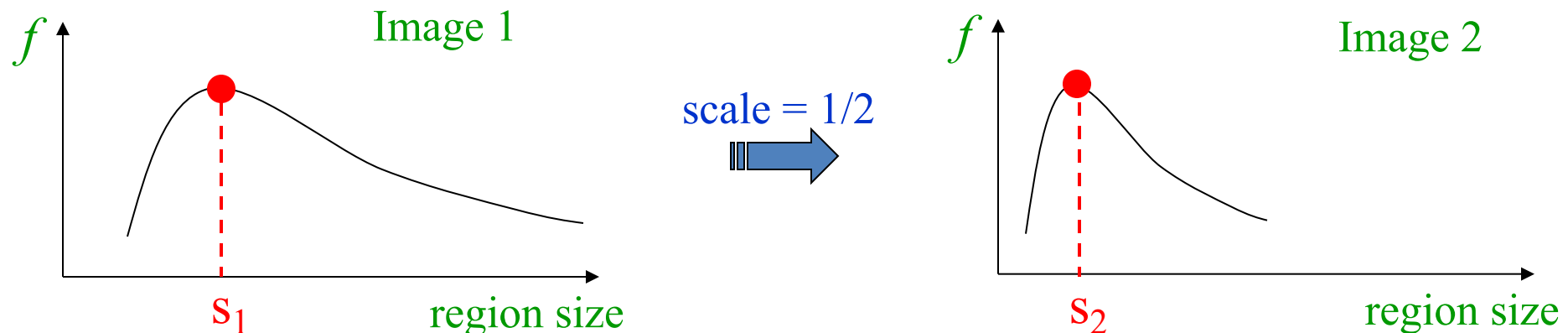
Scale Invariant Detection

- Common approach:

Take a local maximum of this function

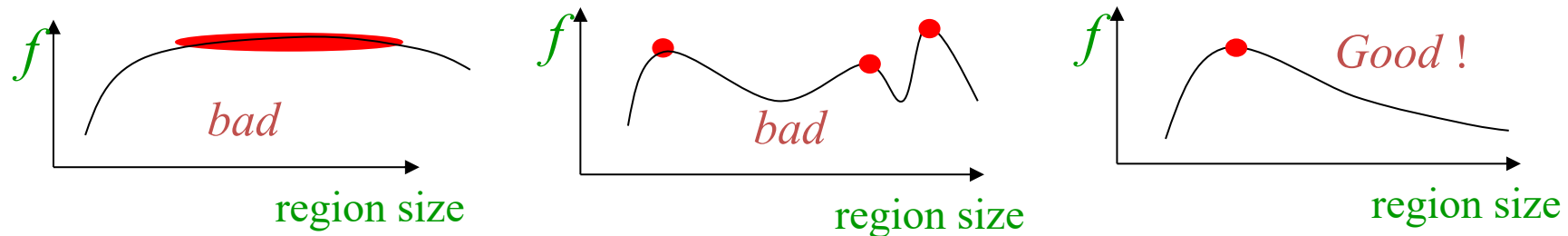
Observation: region size, for which the maximum is achieved, should be *invariant* to image scale.

Important: this scale invariant region size is found in each image **independently!**



Scale Invariant Detection

- A “good” function for scale detection:
has one stable sharp peak



- For usual images: a good function would be a one which responds to contrast (sharp local intensity change)

Scale Invariant Detection

- Functions for determining scale

Kernels:

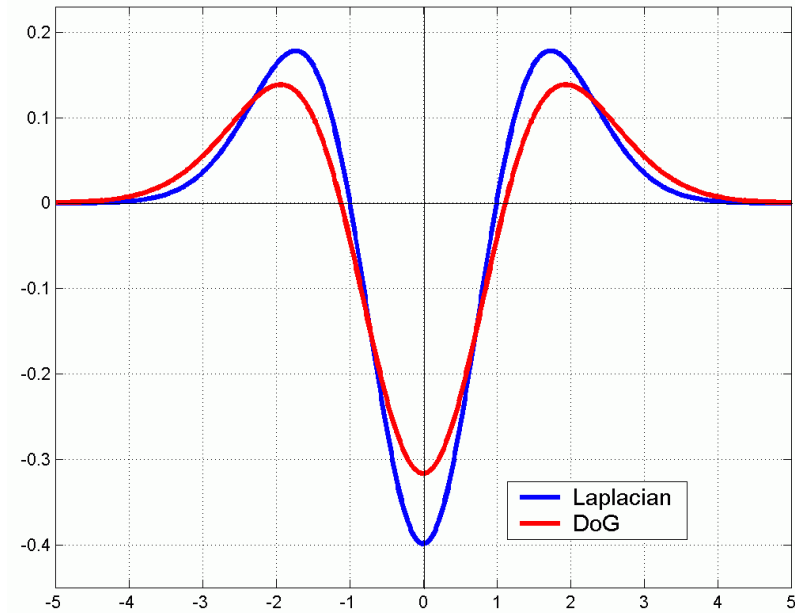
$$DoG = G(x, y, k\sigma) - G(x, y, \sigma)$$

(Difference of Gaussians)

where Gaussian

$$G(x, y, \sigma) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{x^2 + y^2}{2\sigma^2}}$$

$$f = \text{Kernel} * \text{Image}$$



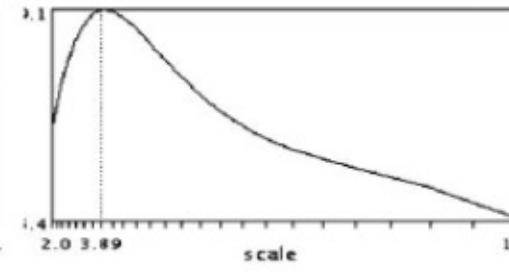
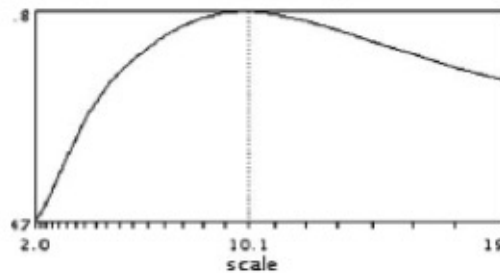
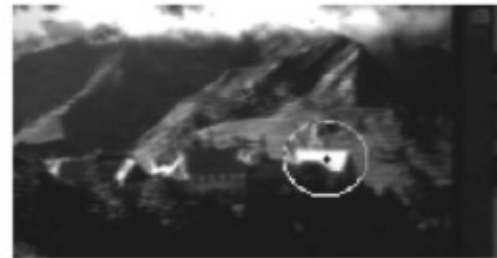
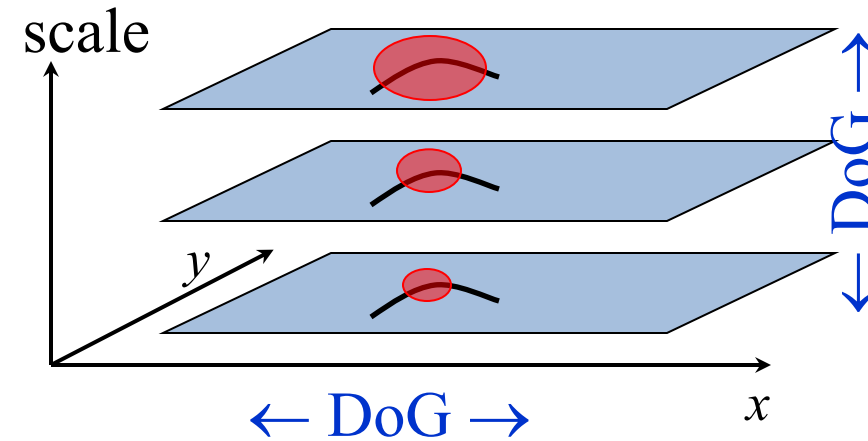
Note: This kernel is invariant to *scale* and *rotation*

Scale Invariant Detectors

- **SIFT**

Find local maximum of:

- Difference of Gaussians in space and scale

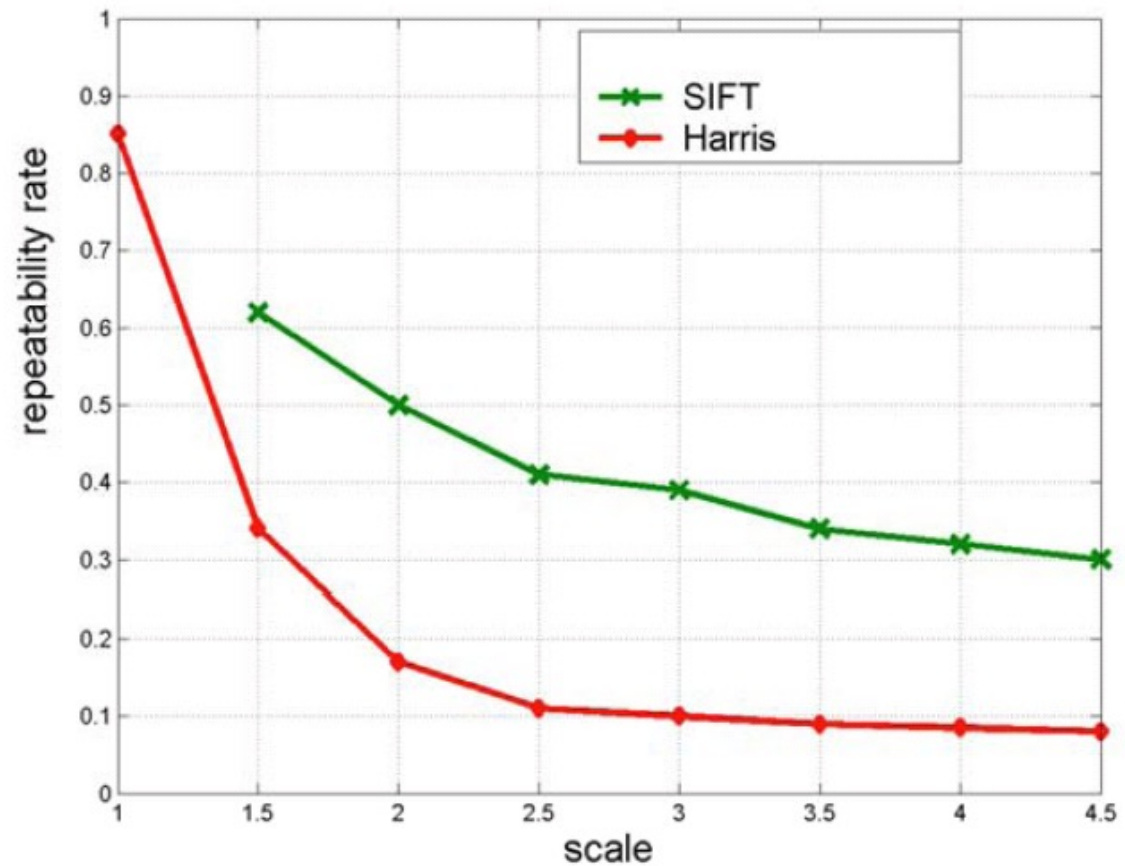
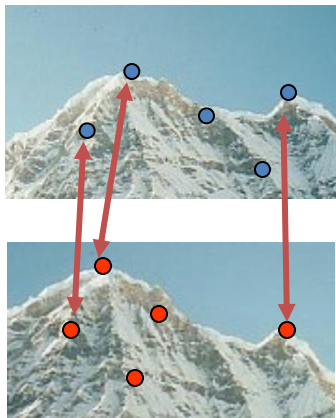


Scale Invariant Detectors

- Experimental evaluation of detectors w.r.t. scale change

Repeatability rate:

$$\frac{\# \text{ correspondences}}{\# \text{ possible correspondences}}$$

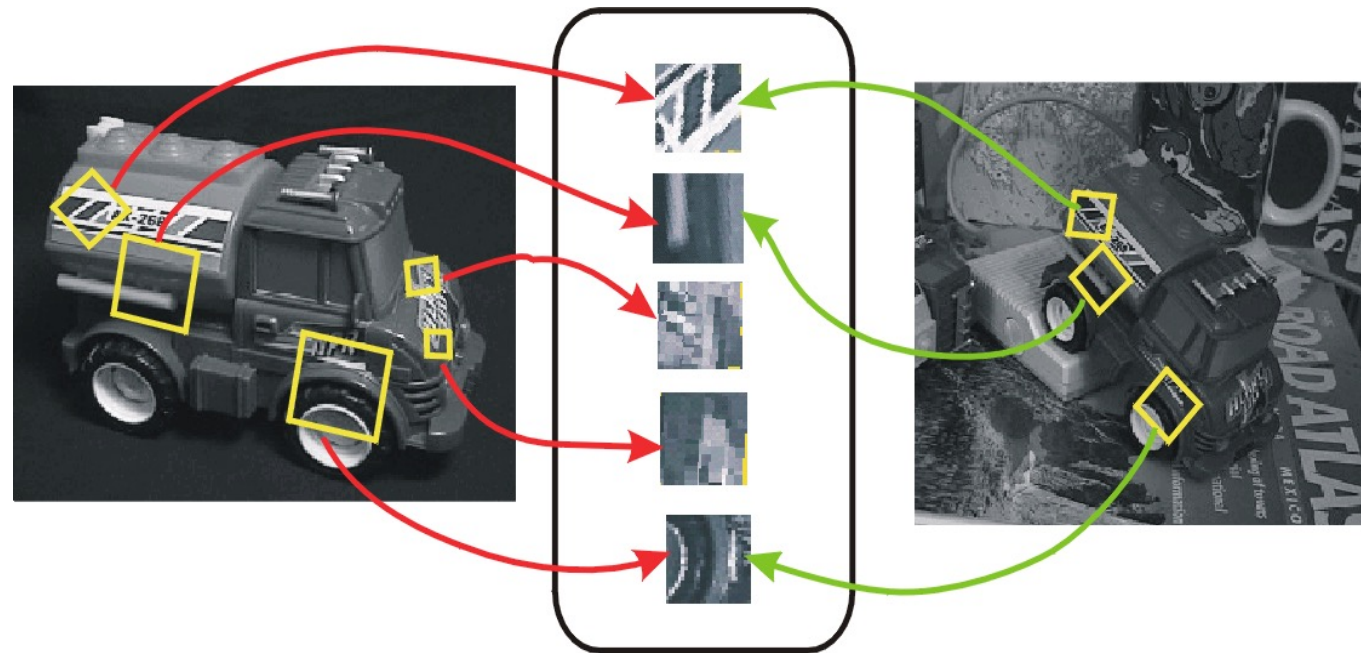


What is SIFT ?

- Scale Invariant Feature Transform (SIFT) is an approach for detecting and extracting local feature descriptors that are reasonably invariant to changes in:
 - rotation
 - scaling
 - small changes in viewpoint
 - illumination

Invariant Local Features

- Image content is transformed into local feature coordinates that are invariant to translation, rotation, scale, and slight view-point and illumination changes



SIFT Descriptor

- SIFT matching features between different images invariant to:
 - Rotation
 - Small image scale
 - Small view point changes
- This is made possible by the use of an opportune feature descriptor (remember, Harris does not use a descriptor for matching)
- What is a descriptor? A descriptor is a “description”, identity card, which allows to recognize a given feature uniquely among many others!

Generation of Keypoint Descriptor

- Keypoint descriptor: computing gradient magnitude and orientation at each image sample point in a region around the keypoint location
- Samples are accumulated into orientation histograms with the length of each bin corresponding to the sum of the gradient magnitudes near that direction within the region.
- The descriptor is therefore a vector containing the values of all the orientations histogram entries
- This vector is normalized to enhance invariance to changes in illumination
- Peaks in the histogram correspond to dominant orientations. If more than one peak is found, a separated feature is assigned to the same point location.
- All the properties of the keypoint are measured relative to the keypoint orientation, this provides invariance to rotation.

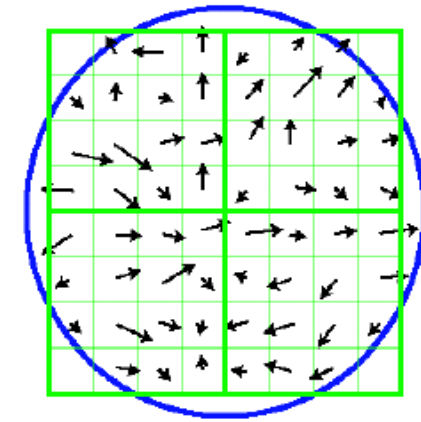
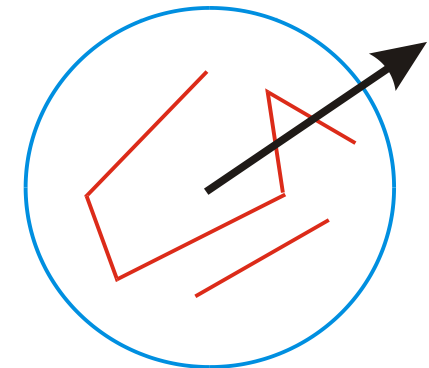
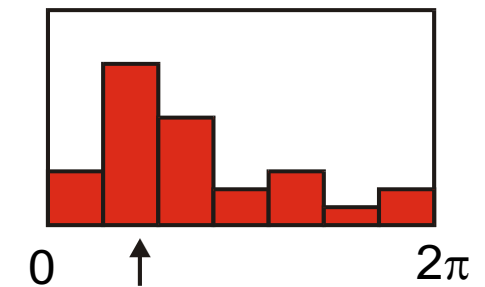
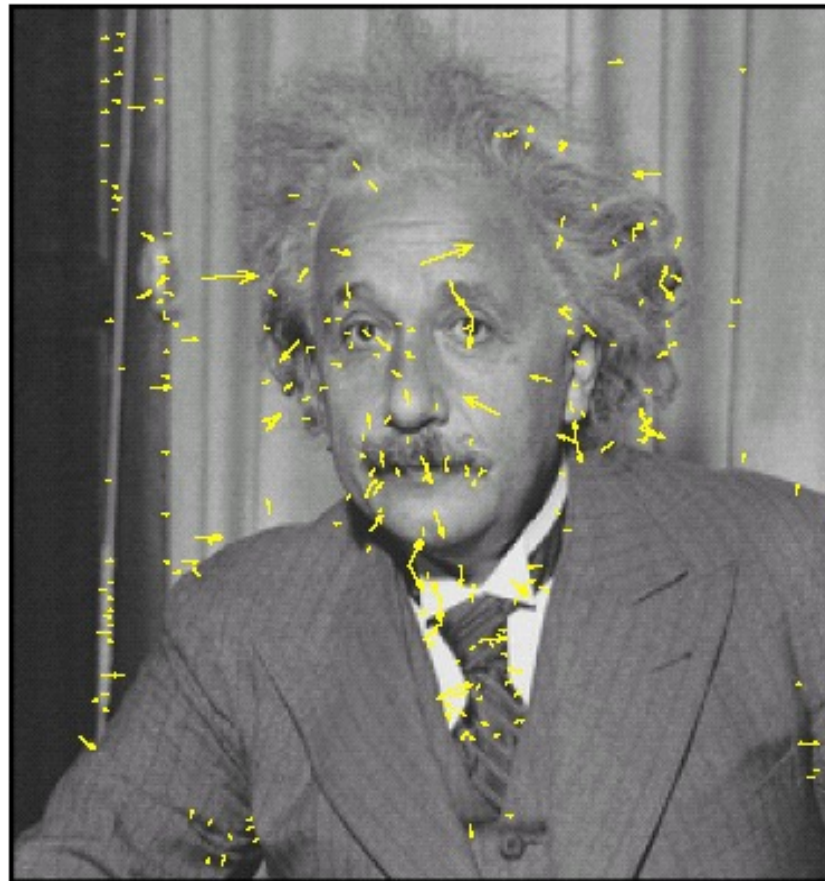


Image gradients

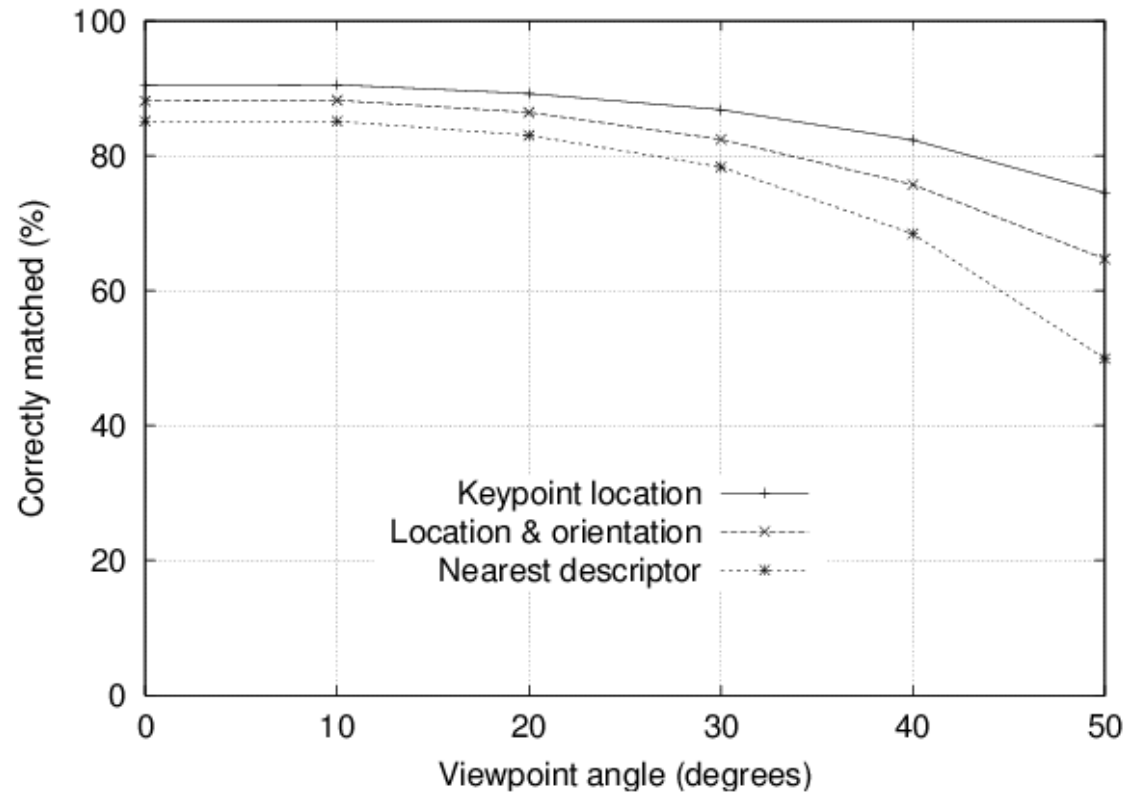


Key point localization

- Final keypoints with selected orientation and scale

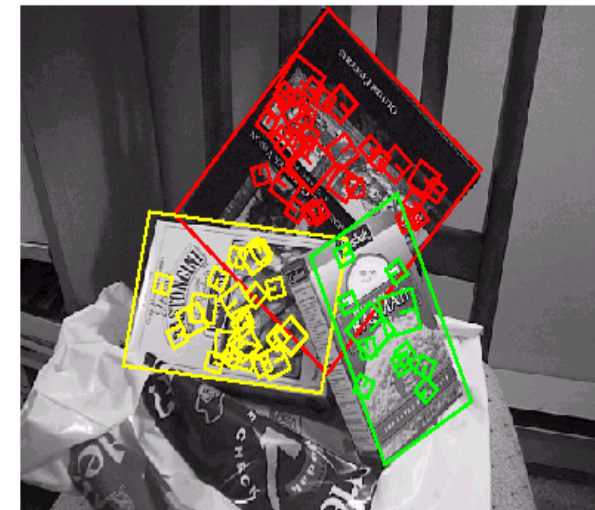


Feature stability to view point change

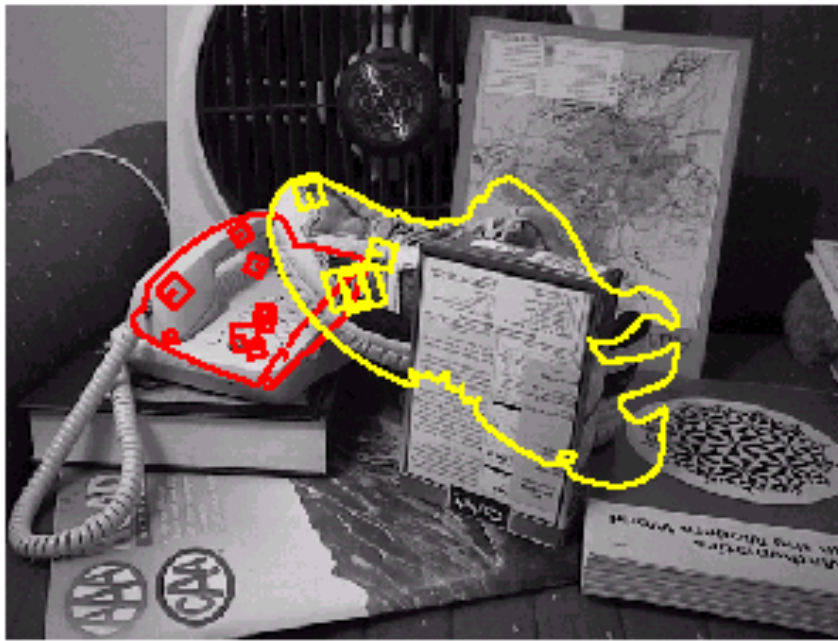


Planar recognition

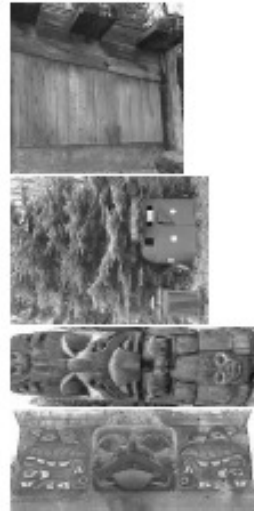
- Planar surfaces can be reliably recognized at a rotation of 60° away from the camera
- Only 3 points are needed for recognition
- But objects need to possess enough texture (i.e. no monochrome objects!)



Recognition under occlusion



Place recognition



Multiple panoramas from an unordered image set

SIFT is used in current consumer cameras and smart phones to build panoramas from multiple shots!



Input images



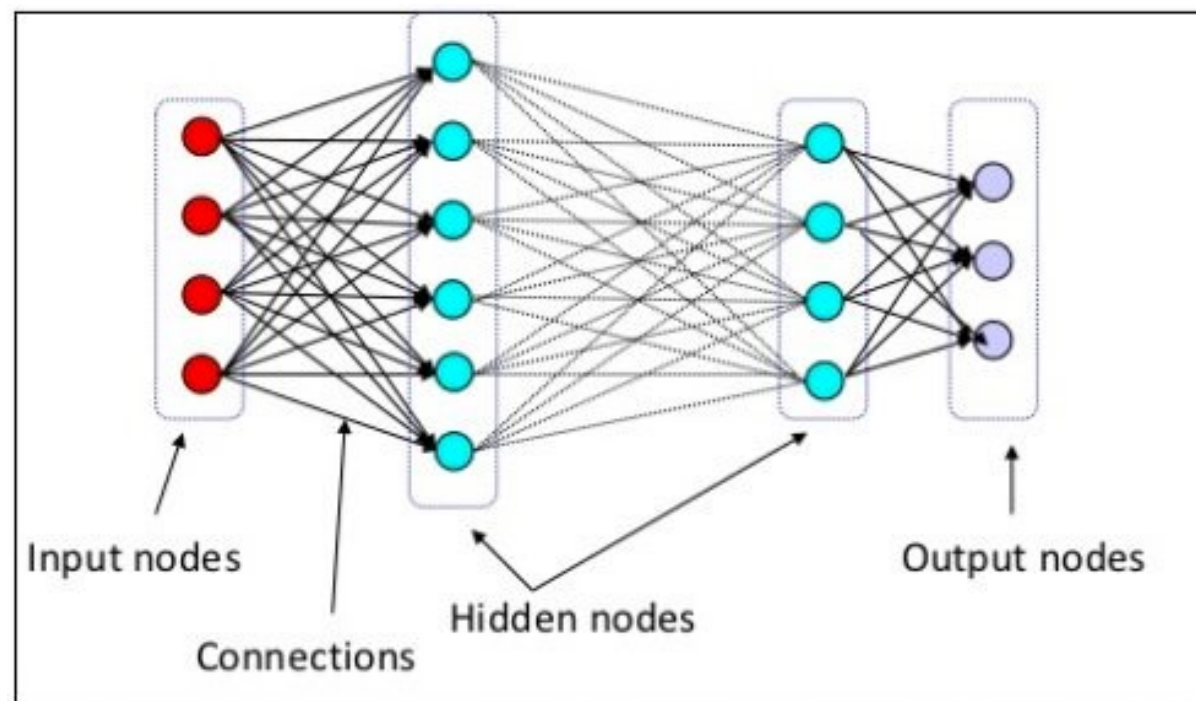
Output panorama 1



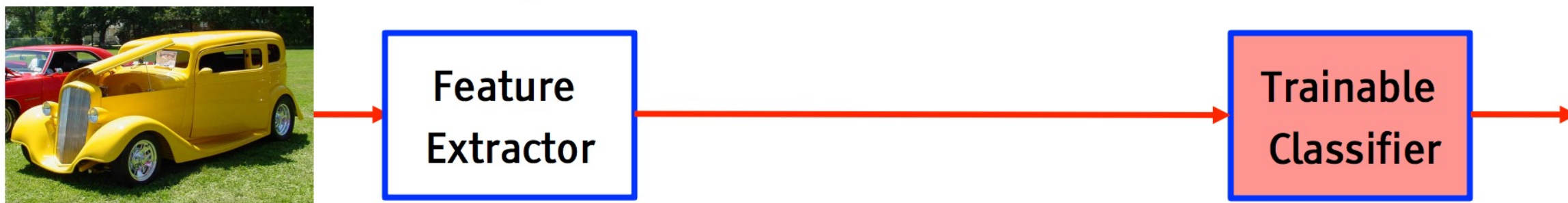
DEEP LEARNING FOR ROBOTIC VISION

Deep Learning

- Hot trend in Machine Learning / AI
- Traditional approaches: Hand tuned features, e.g.:
 - Feature extraction (Computer Vision);
 - Hidden Markov Models & Statistics (Natural Language Processing)
- Deep Learning approach:
 - Learning of parameters for Artificial Neural Network (ANN) based on training data
- Recent success based on:
 - Huge amounts of (training) data
 - Lots of computing power
 - Better DL architectures



Traditional Pattern Recognition: Fixed/Handcrafted Feature Extractor



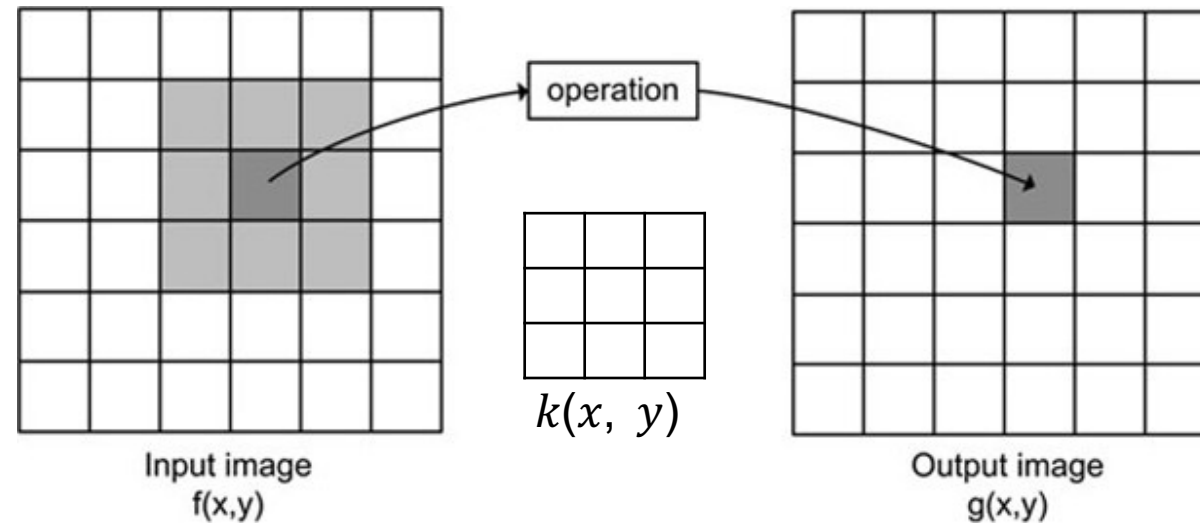
Mainstream Pattern Recognition (until recently)



Deep Learning: Multiple stages/layers trained end to end



Convolution operator



$$g(x, y) = \sum_v \sum_u k(u, v) f(x - u, y - v)$$

(filter, kernel)

Input image

*

Weights



Output image

4	5	7	6	6
3	2	8	0	7
6	7	7	1	5
3	0	1	1	1
4	3	2	1	7

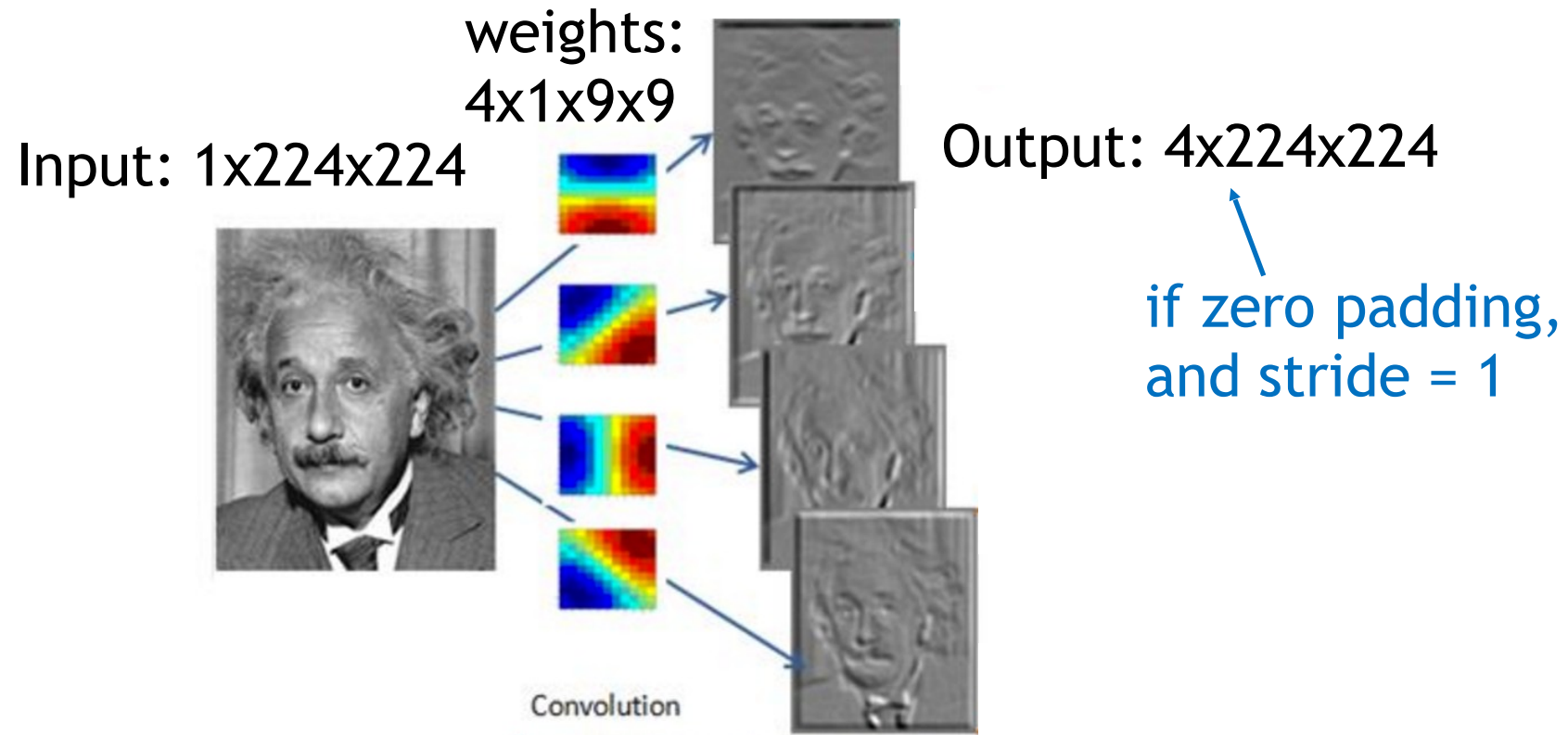
*

0	0	0
1	0	1
0	0	0

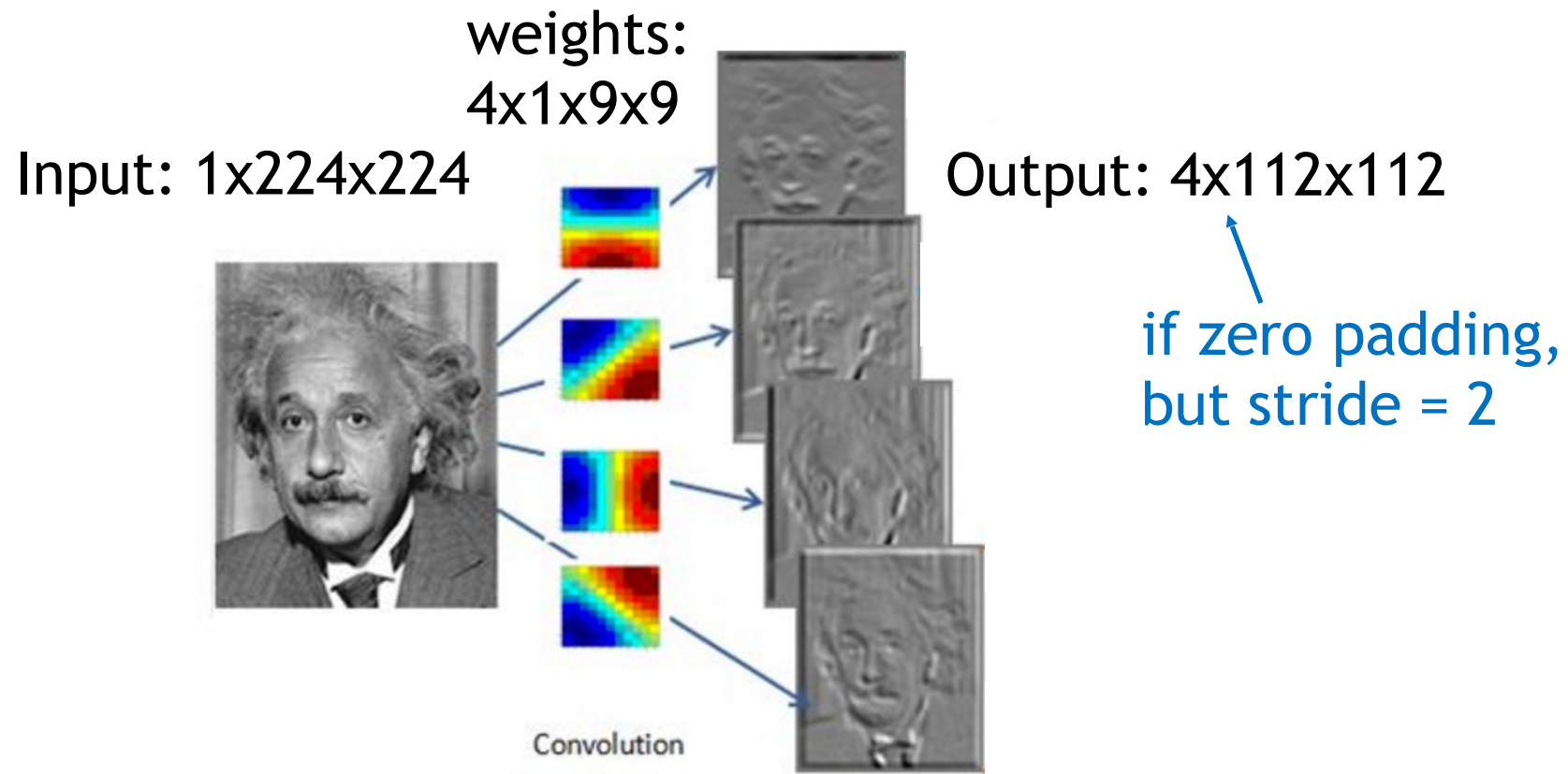


	11	2	15	
	13	8	12	
	?			

Convolutional Layer (with 4 filters)

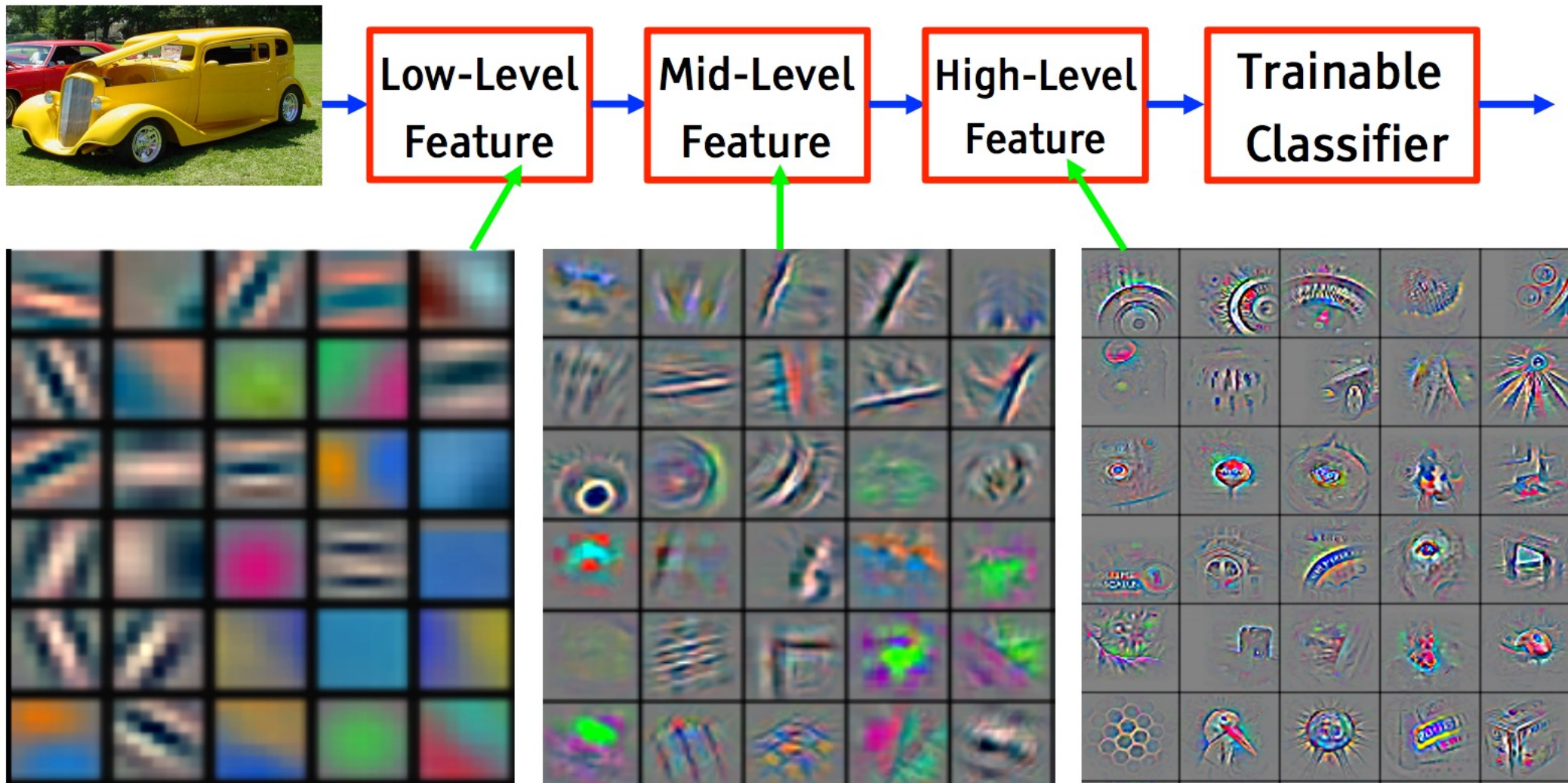


Convolutional Layer (with 4 filters)



Multiple Layers: Levels of Abstraction

Source:
NIPS'2015 Tutorial
Geoff Hinton, Yoshua Bengio & Yann LeCun



Alexnet

ImageNet Classification with Deep Convolutional Neural Networks

Alex Krizhevsky
University of Toronto
kriz@cs.utoronto.ca

Ilya Sutskever
University of Toronto
ilya@cs.utoronto.ca

Geoffrey E. Hinton
University of Toronto
hinton@cs.utoronto.ca

the paper that started the
deep learning revolution!

Image Classification

Classify an image into 1000 possible classes:

e.g. Abyssinian cat, Bulldog, French Terrier, Cormorant,
Chickadee,

red fox, banjo, barbell, hourglass, knot, maze, viaduct, etc.



cat, tabby cat(0.71)

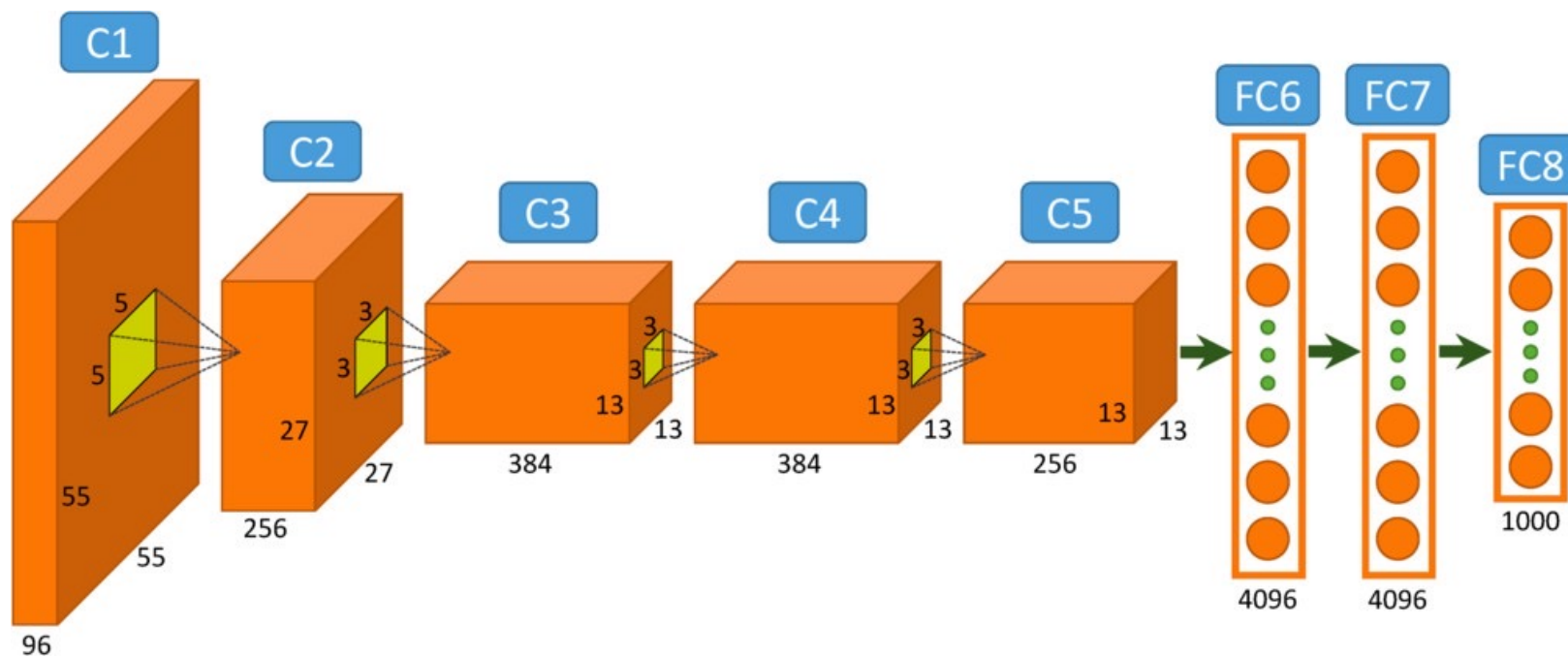
Egyptian cat (0.22)

red fox (0.11)

.....

train on the ImageNet
challenge dataset,
~1.2 million images

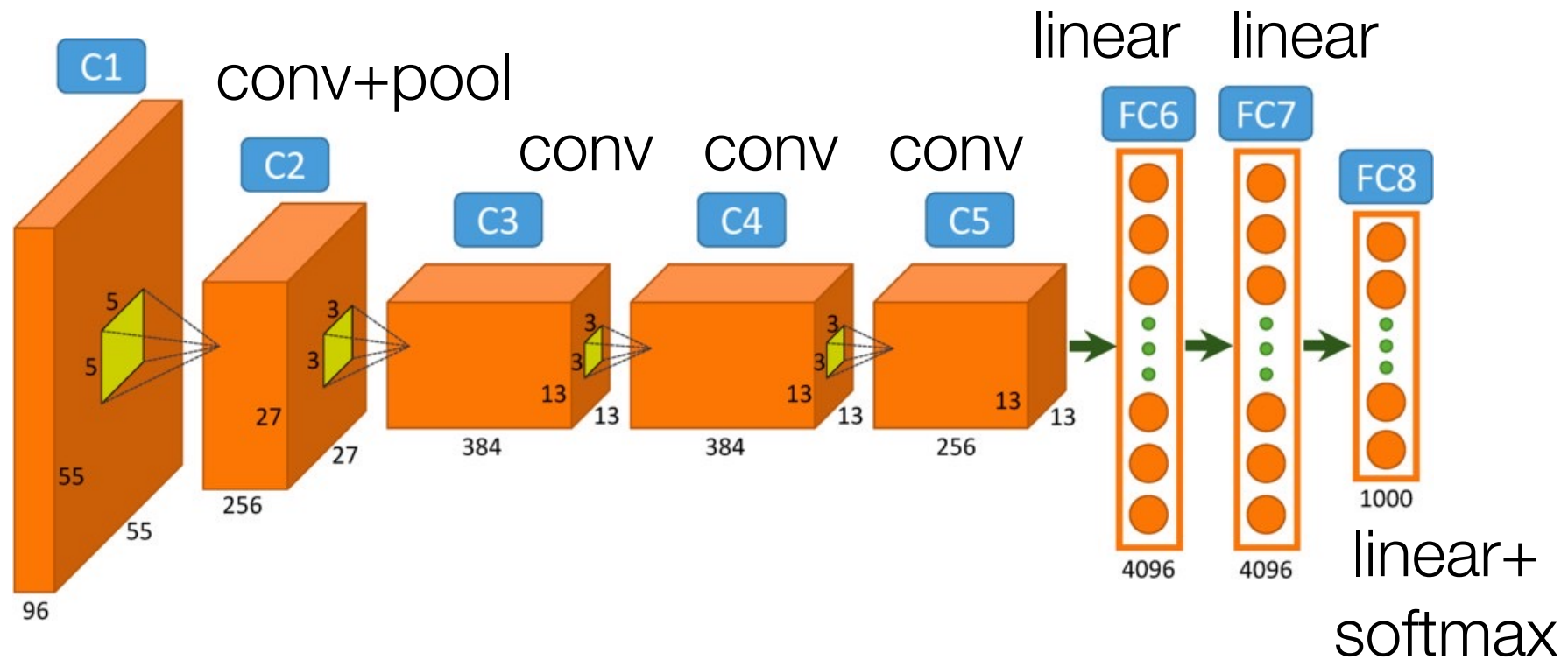
Alexnet



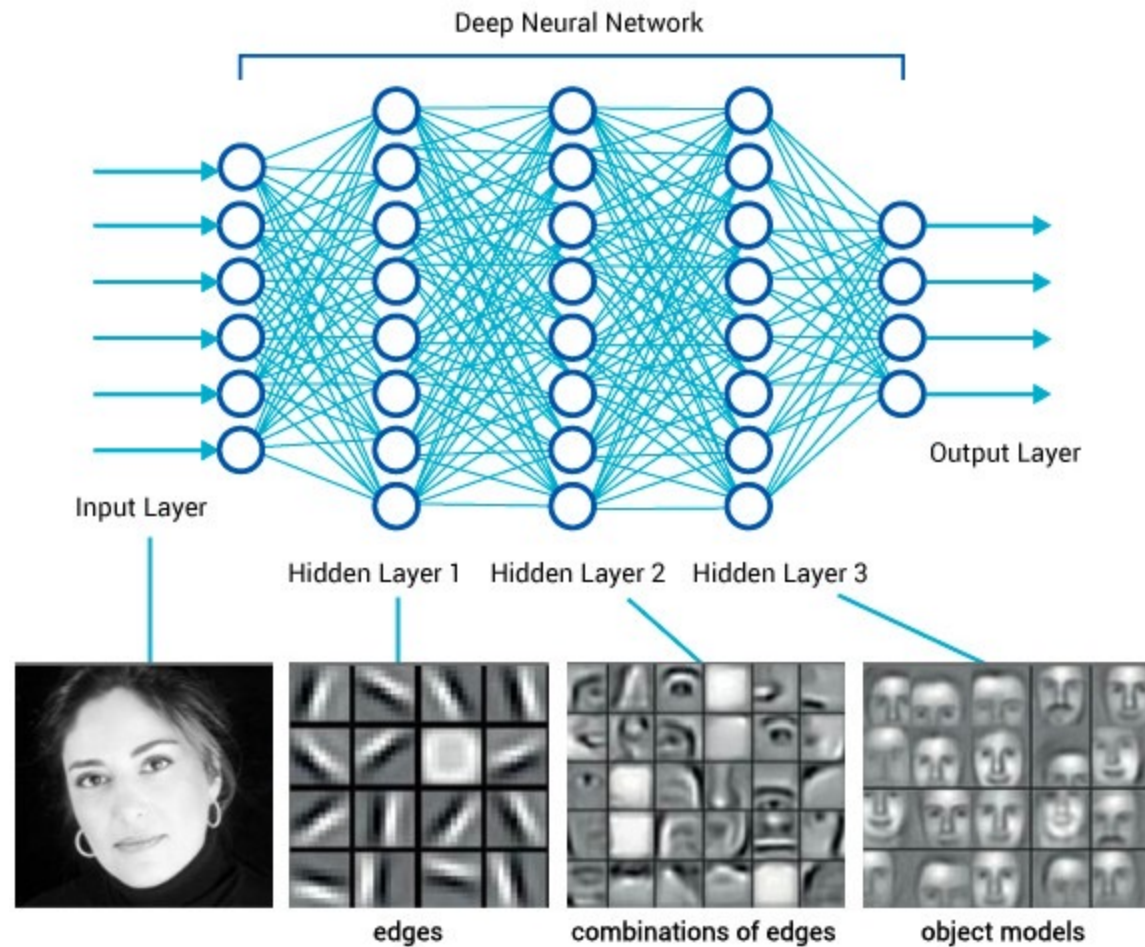
<https://www.saagie.com/fr/blog/object-detection-part1>

Alexnet

conv+pool

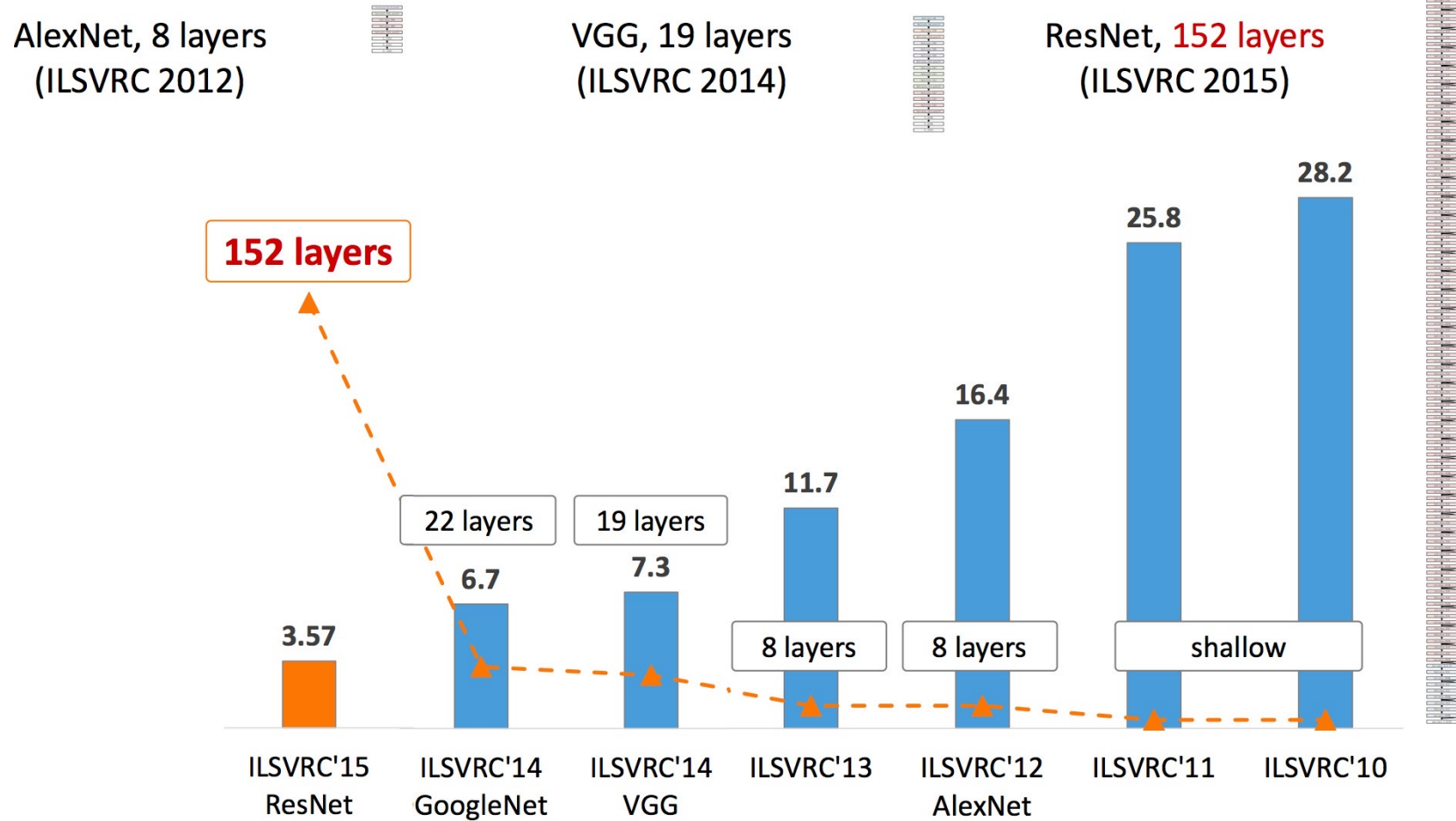


What is happening?



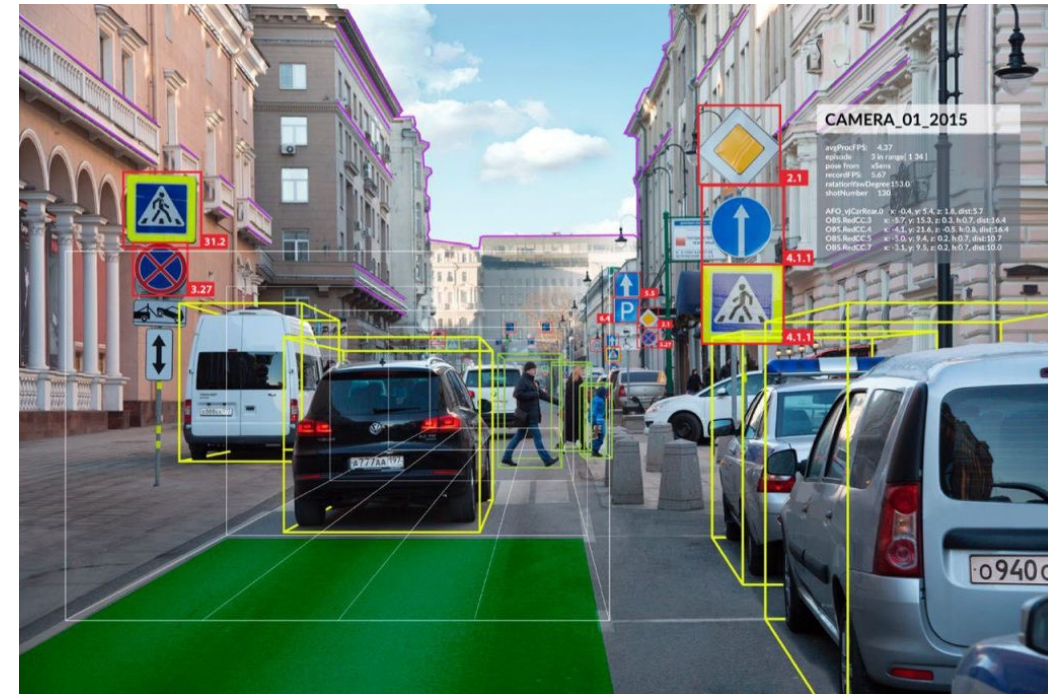
<https://www.saagie.com/fr/blog/object-detection-part1>

Revolution of Depth



Computer Vision in Autonomous Driving

- DL for Computer Vision for detection of:
 - Cars (Truck; Bus; Police car!; ...)
 - Pedestrian; Bicycle; ...
 - Lane; curb
 - Markings on the road
 - Traffic Signs
 - Traffic Lights
- From Cameras AND Lidars



<https://becominghuman.ai/computer-vision-applications-in-self-driving-cars-610561e14118>

Computer Vision for Robotics

- DL for Computer Vision for detection of:
 - Doors; Door handle
 - Signs; Read door signs
 - Objects
 - Other Robots



Amazon Picking Challenge

- Robot stow and take (pick) products from shelves
- Challenges in: Computer vision (find object and its pose [position & orientation]) and Manipulation (planning, grasping)
- Since 2015 – now co-located with RoboCup
- Winner 2016: Team Delft
 - Suction gripper (easy!)
 - 100 items per hour (human: 400)
 - Failure rate: 16.7 %
 - Deep learning to find objects:
 - Stereo camera for 3D
 - ROS Industrial

<https://www.theverge.com/2016/7/5/12095788/amazon-picking-robot-challenge-2016>



Deep Learning for Scene Understanding

- Semantics Segmentation
 1. single RGB image as input
 2. semantic labeling at pixel-level
 3. divide scene to different regions and objects
 - semantic SLAM
 - help to remove dynamic object (Chen et al. SuMa++)
 - provide cues for loop closing (Chen et al. OverlapNet)



Poudel, Rudra PK, Stephan Liwicki, and Roberto Cipolla. "Fast-scnn: Fast semantic segmentation network." arXiv preprint arXiv:1902.04502 (2019).

Guo, Jian, et al. "GluonCV and GluonNLP: Deep Learning in Computer Vision and Natural Language Processing." Journal of Machine Learning Research 21.23 (2020): 1-7.

Deep Learning for Feature Extraction

- Optical Flow Estimation

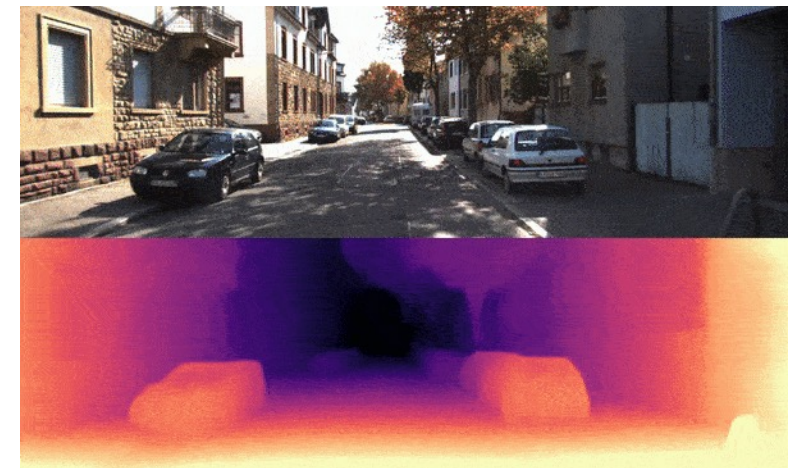
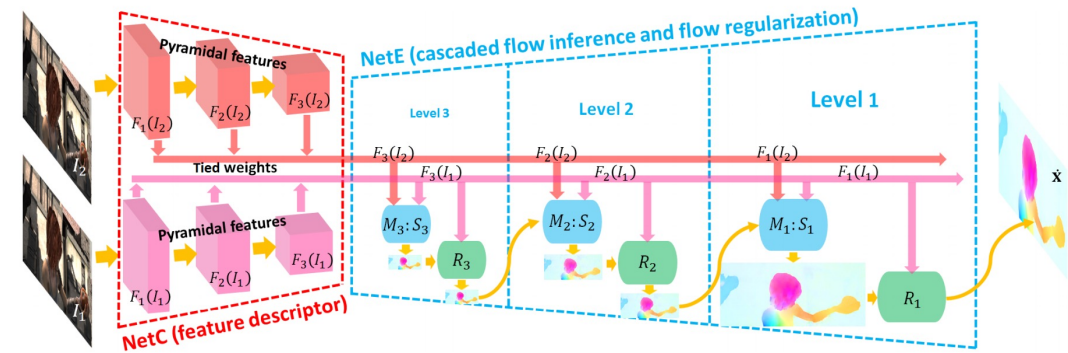
1. two frames as input
2. output the optical flow
3. generating the 2D-2D correspondences

- Monocular Depth Estimation

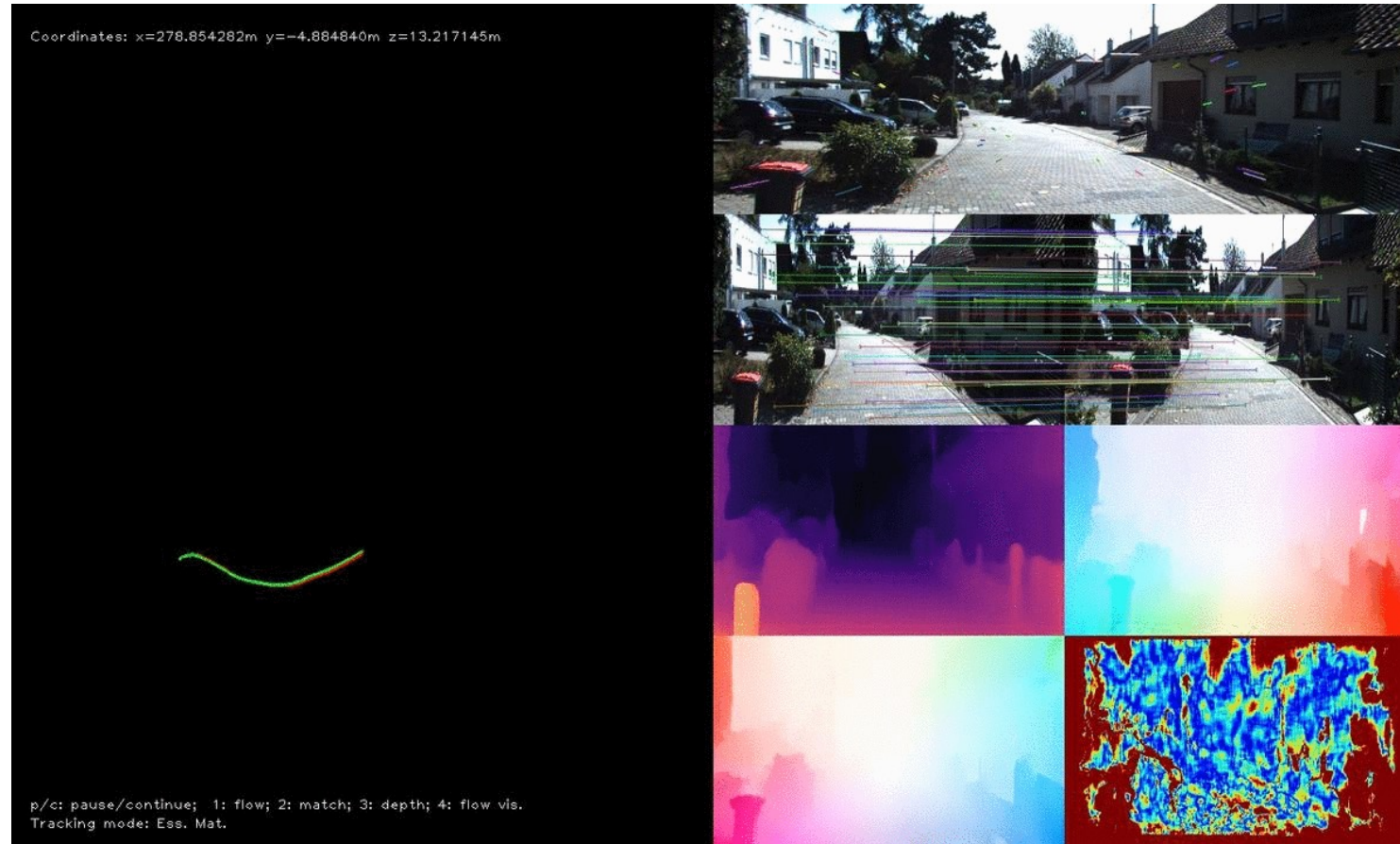
1. single RGB image as input
2. output the depth map
3. provides 3D information, recover scaling factor

Hui, Tak-Wai, Xiaoou Tang, and Chen Change Loy. "Liteflownet: A lightweight convolutional neural network for optical flow estimation." Proceedings of the IEEE conference on computer vision and pattern recognition. 2018.

Godard, Clément, et al. "Digging into self-supervised monocular depth estimation." Proceedings of the IEEE international conference on computer vision. 2019.



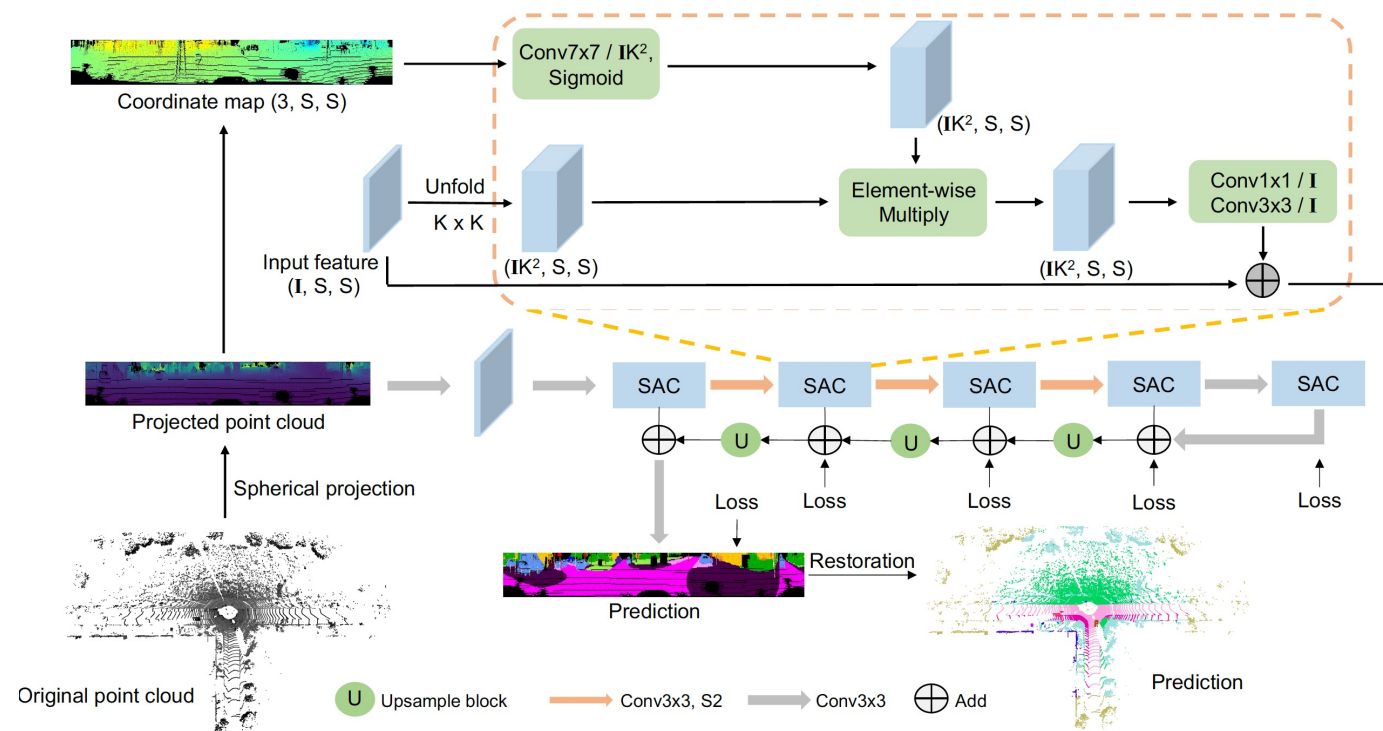
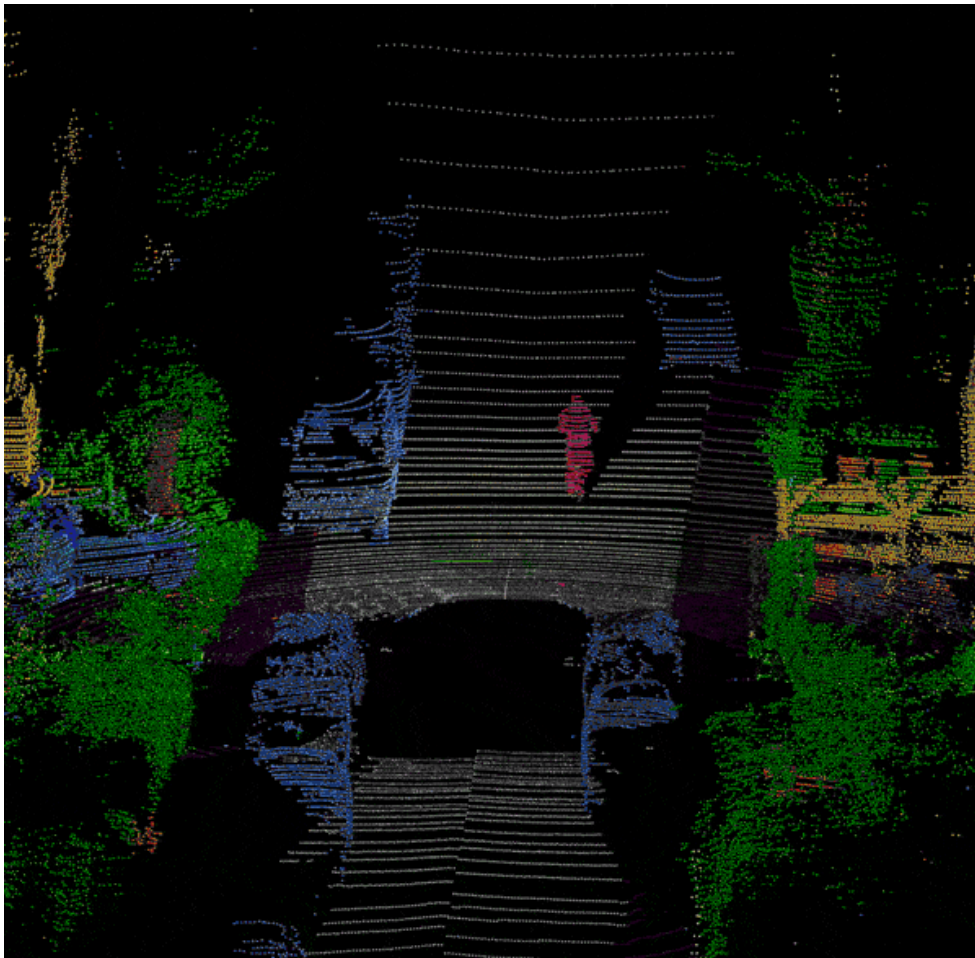
Deep Learning in Visual Odometry



Zhan, Huangying, et al. "Visual odometry revisited: What should be learnt?." 2020 IEEE International Conference on Robotics and Automation (ICRA). IEEE, 2020.

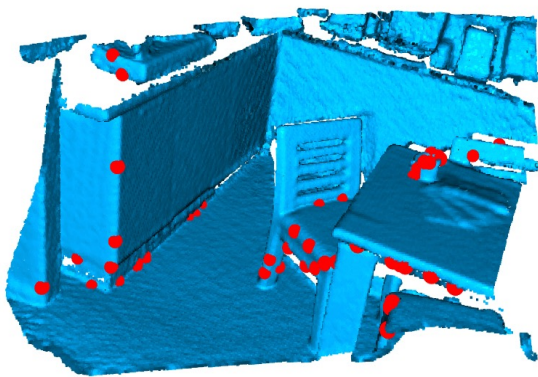
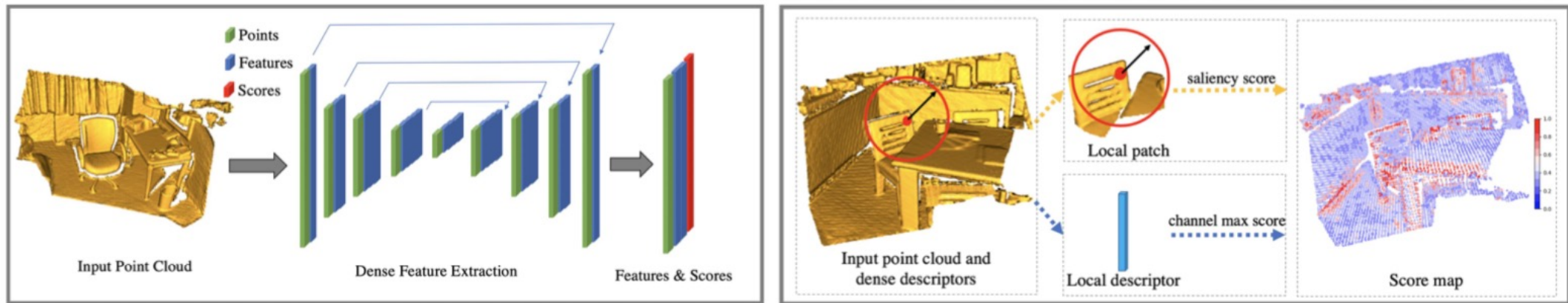
Point Cloud Segmentation

- "SqueezeSegV3: Spatially-Adaptive Convolution for Efficient Point-Cloud Segmentation." Chenfeng Xu, Bichen Wu, Zining Wang, Wei Zhan, Peter Vajda, Kurt Keutzer, and Masayoshi Tomizuka.

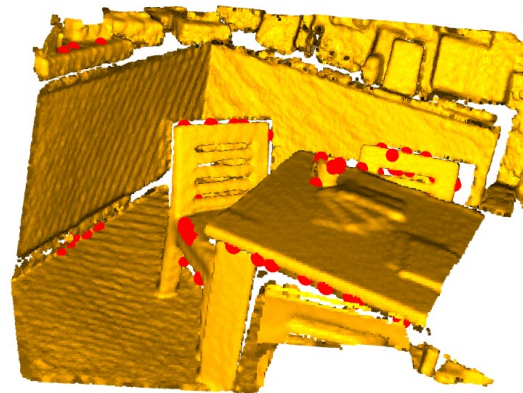


Feature Descriptors => Registration

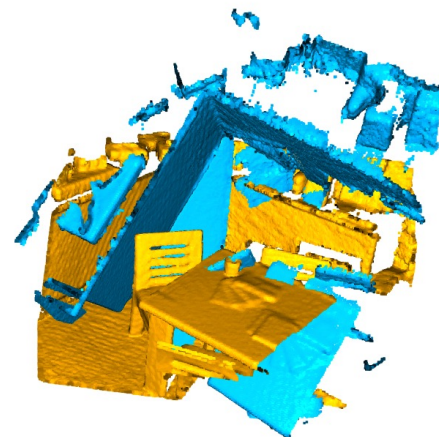
- "D3Feat: Joint Learning of Dense Detection and Description of 3D Local Features", by Xuyang Bai, Zixin Luo, Lei Zhou, Hongbo Fu, Long Quan and Chiew-Lan Tai.



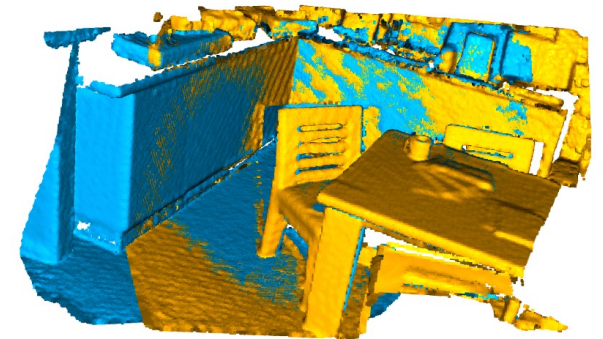
Source point cloud



Target point cloud



Initial State



Registered using D3Feat + RANSAC

Vision Language Models

Transformer encoders for vision

Mohit Iyyer

College of Information and Computer Sciences University of
Massachusetts Amherst

https://people.cs.umass.edu/~miyyer/cs685/slides/vision_nlp.pdf

Image captioning



a red truck is
parked on a street
lined with trees

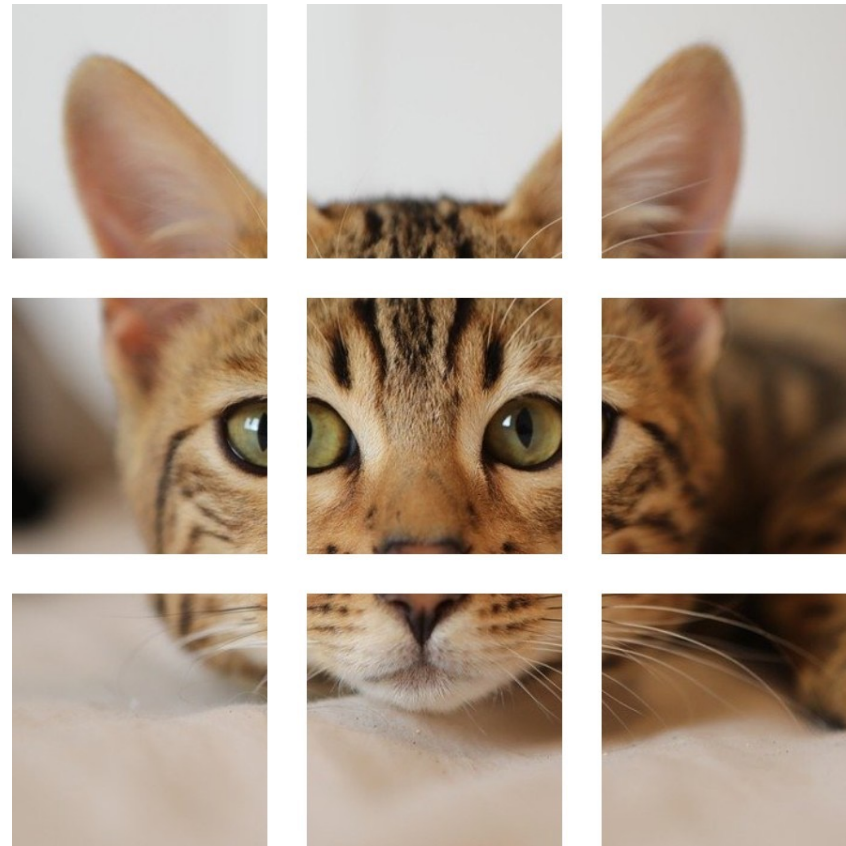
Visual question answering

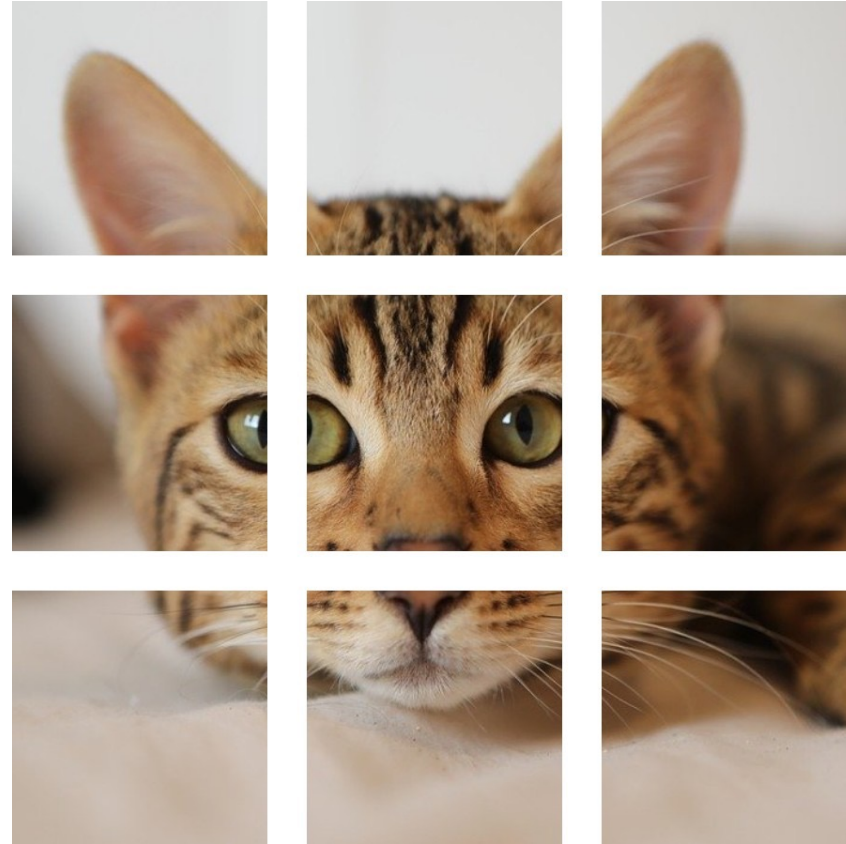


- Is this truck considered “vintage”?
- Does the road look new?
- What kind of tree is behind the truck?

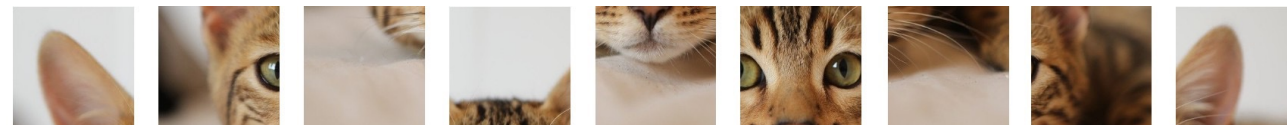
Self-attention on pixels





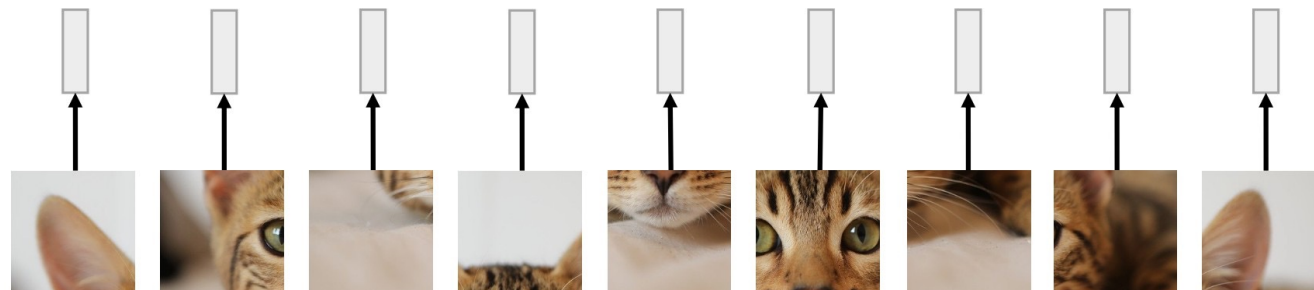


N input patches, each
of shape 3x16x16



Linear projection to
D-dimensional vector

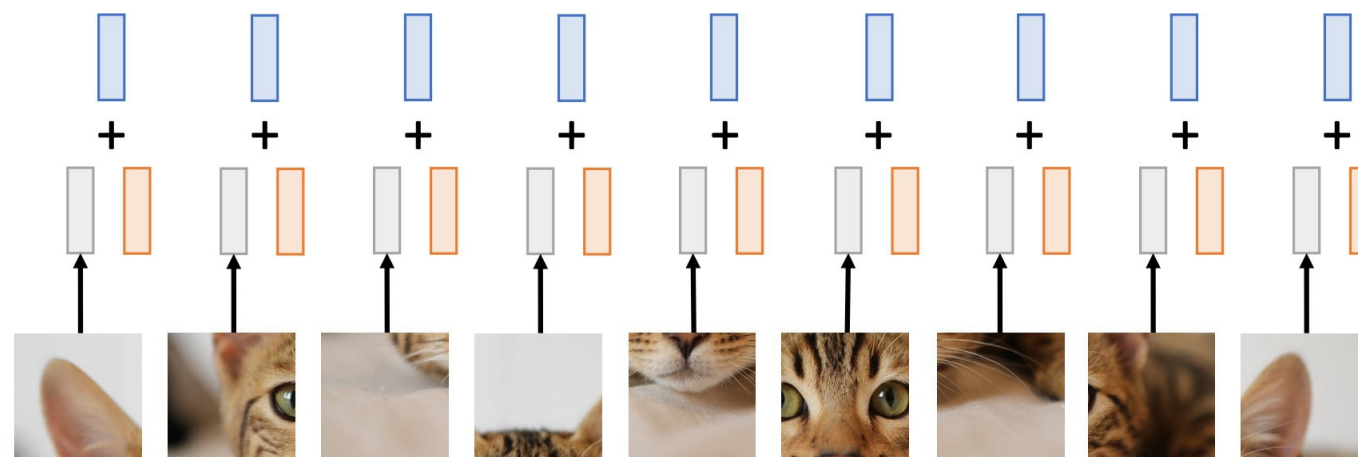
N input patches, each
of shape 3x16x16

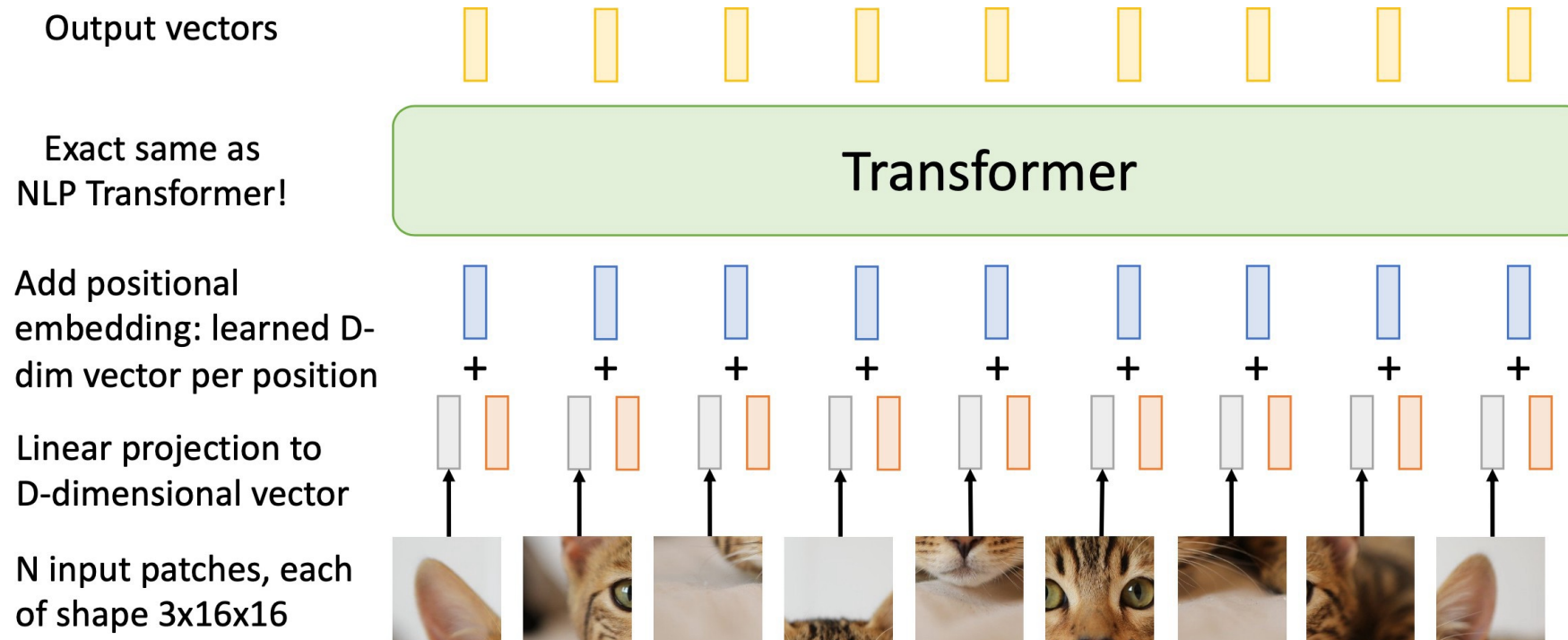


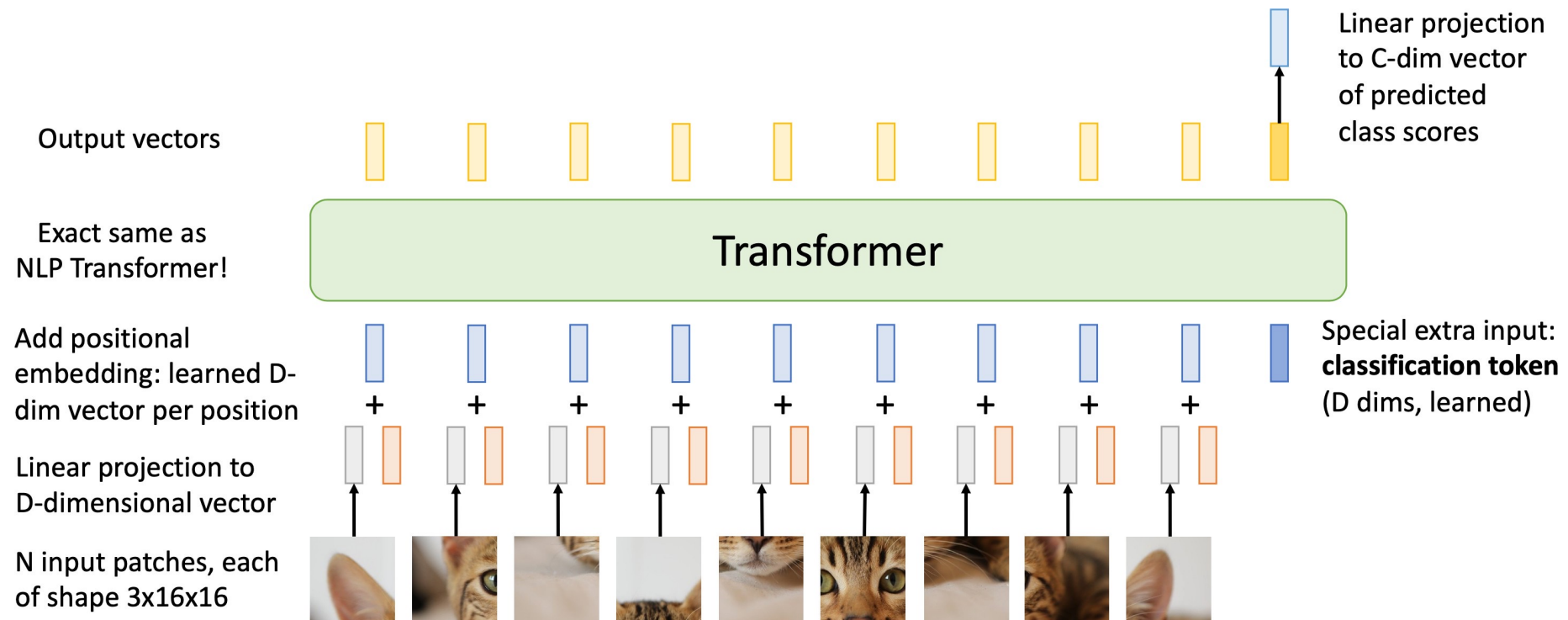
Add positional
embedding: learned D-
dim vector per position

Linear projection to
D-dimensional vector

N input patches, each
of shape 3x16x16

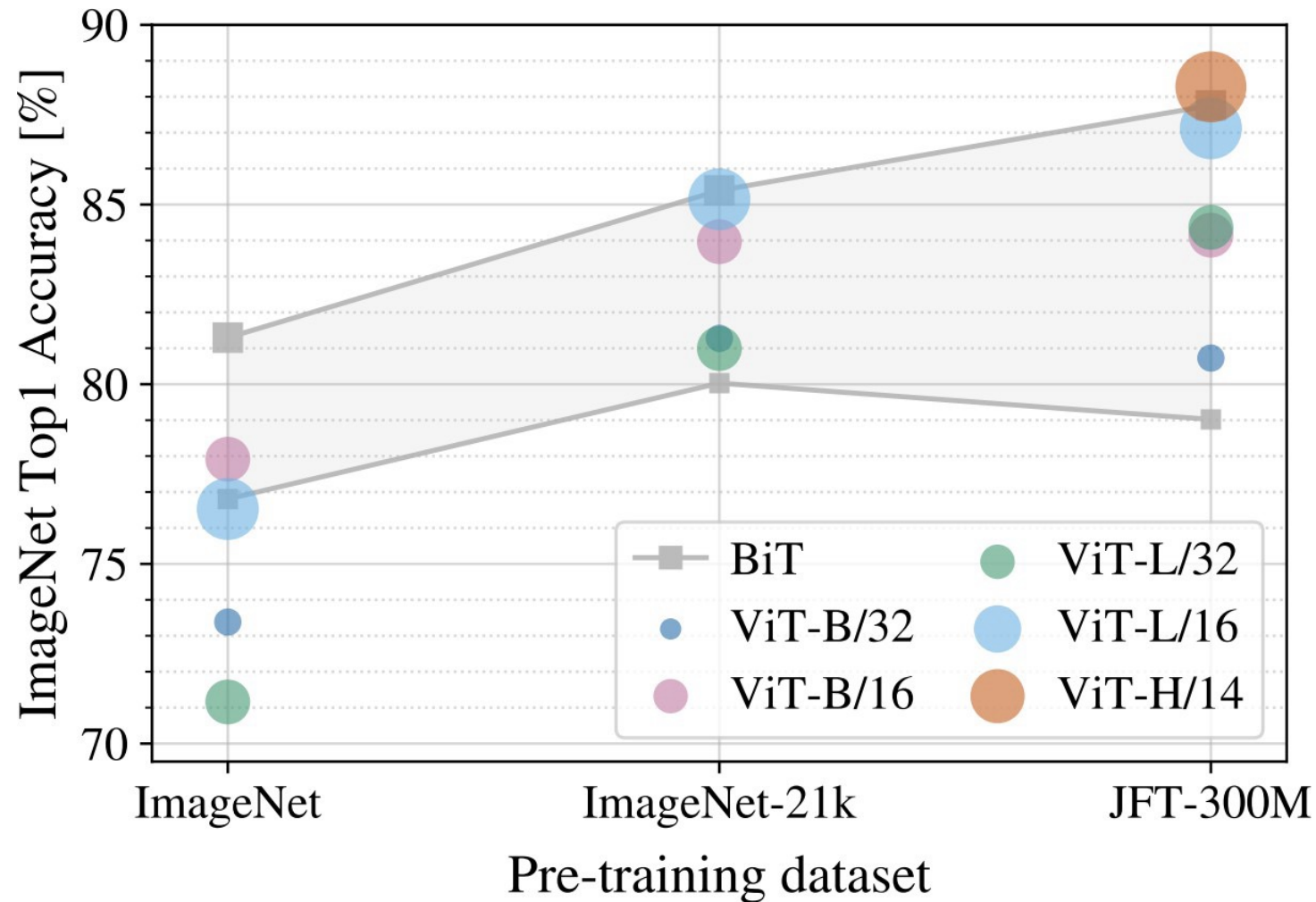






16x16 patches = $16*16*3 =$
768d embedding

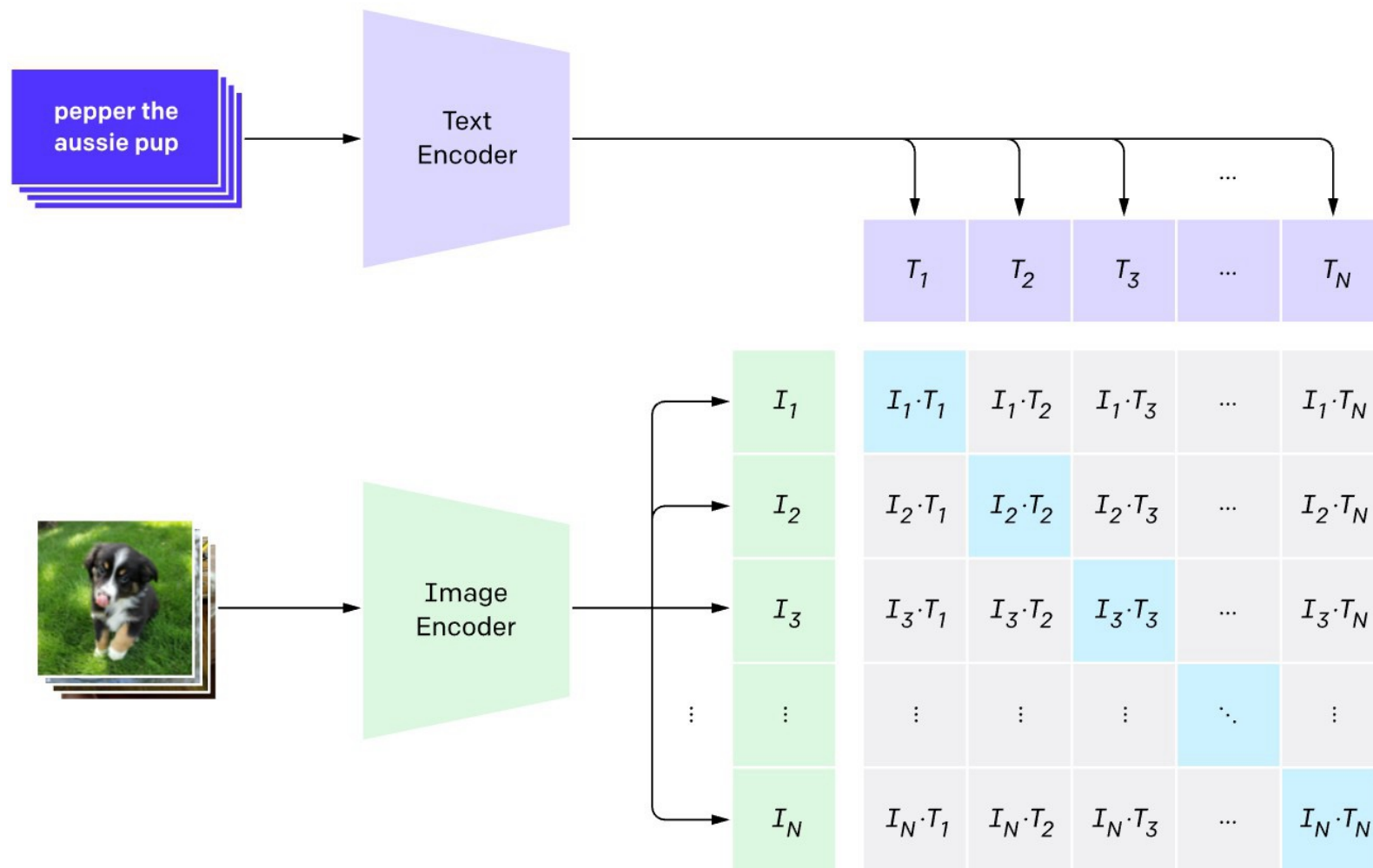
Vision Transformers (ViT) outperform ResNets with larger datasets



OpenAI's CLIP: Contrastive language-image pretraining

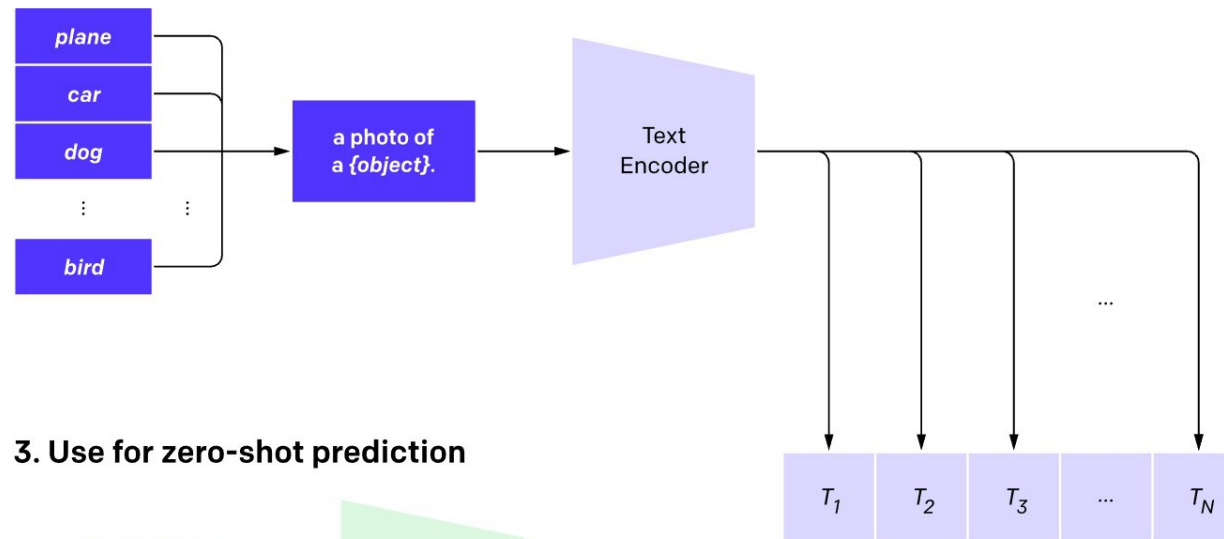
- OpenAI collect 400 million (image, text) pairs from the web
- Then, they train an image encoder and a text encoder with a simple contrastive loss: given a collection of images and text, predict which (image, text) pairs actually occurred in the dataset

1. Contrastive pre-training

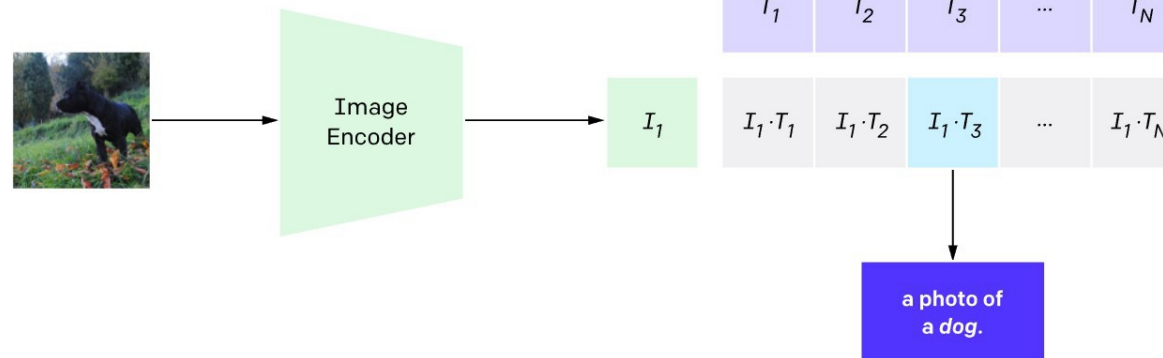





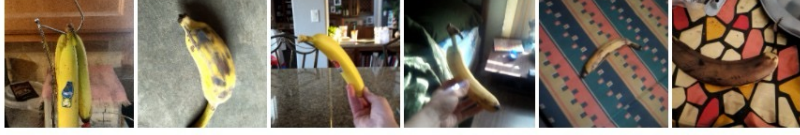
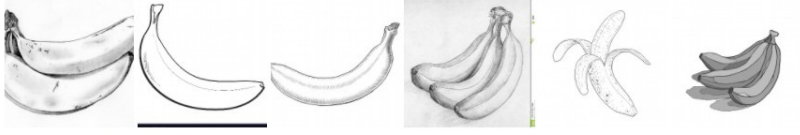
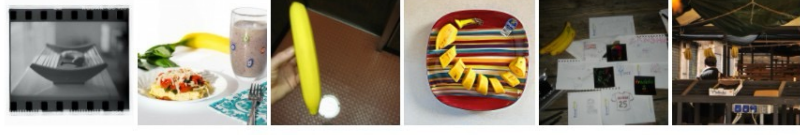
Similar to GPT-3, you can use CLIP for zero-shot learning

2. Create dataset classifier from label text

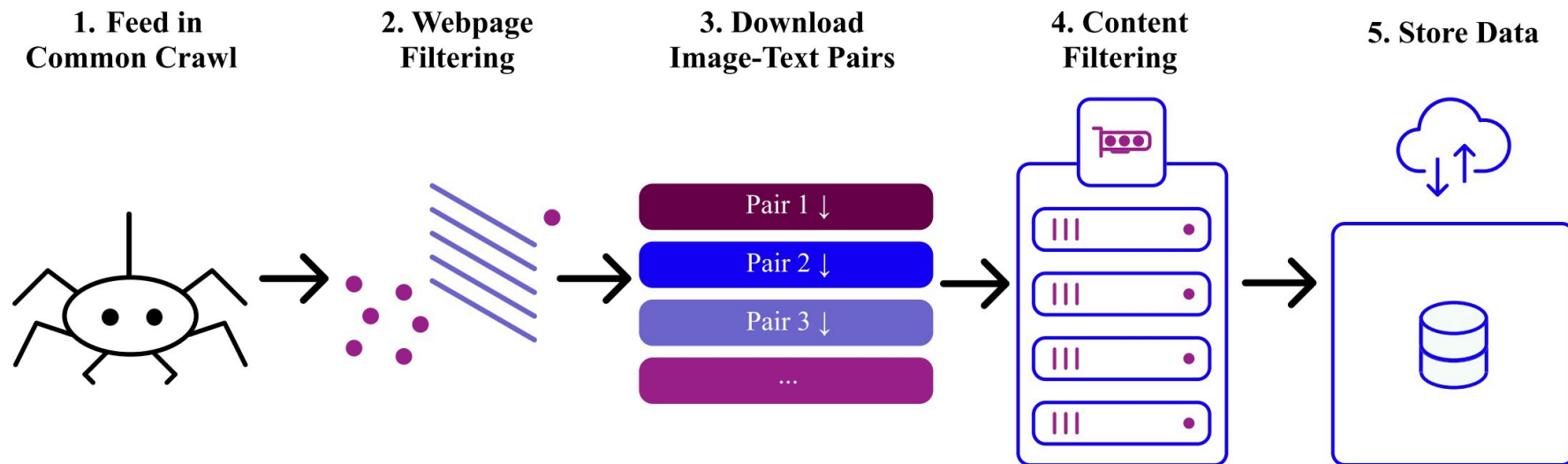


3. Use for zero-shot prediction



DATASET	IMAGENET RESNET101	CLIP VIT-L
 <p>ImageNet</p>	76.2%	76.2%
 <p>ImageNet V2</p>	64.3%	70.1%
 <p>ImageNet Rendition</p>	37.7%	88.9%
 <p>ObjectNet</p>	32.6%	72.3%
 <p>ImageNet Sketch</p>	25.2%	60.2%
 <p>ImageNet Adversarial</p>	2.7%	77.1%

LAION-5B: a dataset of 5 billion image/text pairs!



Major copyright issues...

Stable Diffusion and other image-generating AI products could not exist without the work of painters, illustrators, photographers, sculptors, and other artists. Stable Diffusion was trained on the [LAION-5B](#) dataset. LAION-5B contains 5.85 billion image-text pairs. Most of the images contained in the dataset are copyrighted, and LAION claims no ownership in them. As it notes, “The images are under their copyright.”